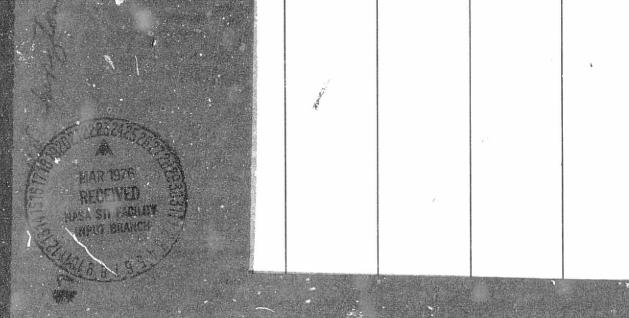
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# Sound and Vibration Research Laboratory

SEATTLE, WASHINGTON 98198

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# Final Report on

NASA Grant No. NGR-002-144

NC-R-48-602-144

# A STUDY OF SOUND GENERATION IN SUBSONIC ROTORS

Report No. ME 73-11

Volume 2 of 2

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#### 1.0 INTRODUCTION

Volume 2 of the final report is used to outline four computer programs which were developed during the grant period. All were coded in FORTRAN IV Language for usage on the University of Washington CDC 6400 digital computer.

The discussions here are primarily user input instructions. For two of the programs, ROTOR and AIRFOIL, the background models are developed in some detail in Volume 1 of the report. Program TONE is developed herein and SDATA is outlined here with reference to the literature where the detailed development requires a book to describe. The function of each program is discussed below.

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- (1) Program AIRFOIL: This program computes the spectrum of radiated sound from a single airfoil immersed in a laminar flow field. The machanism is force fluctuations which are related to the unsteady wake momentum. Input required is the aerodynamic properties of the turbulent wake.
- (2) Program ROTOR: The purpose of program ROTOR is to provide an extension of the single airfoil in AIRFOIL to a rotating frame. This is a model for sound generation in subsonic rotors. The only broad band mechanism currently in the program is the airfoil wake mechanism. Program ROTOR also computes tone sound generation due to the steady state forces on the blades (the Gutin result). Input requirements are similar to those for AIRFOIL.

- (3) Program TONE: A moving source analysis is used to generate a time series for an array of forces moving in a circular path as would be the case for a rotor. This analysis has great flexibility in that arbitrary blade spacings, blade forces and source motions can be easily accommodated. Broad band effects have been included using autoregression methods. The resultant time series are Fourier transformed using a Fast Fourier Transform to present the sound radiation in the more normal spectral form. With some study, a user can make this program a very valuable tool in sound generation investigations.
- (4) Program SDATA: This program is a standard time series analysis package. It will read in two discrete time series and form auto and cross covariances and normalize these to form correlations. The program will then transform the covariances to yield auto and cross power spectra by means of a Fourier transformation. The spectral data are presented in terms of amplitude and phase as well as the coherency spectrum.

A final note on these programs is in order. These were developed as tools to be used in the work performed under the grant. There was no intention to provide the programs as complete packages for general usage. The content is general enough, however, that with some effort a user should be able to employ the programs to advantage. He is cautioned to understand the analytical models before he becomes too involved in turning around decks. No program is a substitute for this understanding. Tools must be skillfully used.

To the end of providing a usable tool the programs are coded in variable names which read very like those of the physical variables they represent. For example the density will be RHO and the longitudinal turbulence covariance will be UlUl, etc. This should facilitate the reading of the program listings.

Each of the programs is discussed in the following sections.

#### 2.0 PROGRAM AIRFCIL

The fortran program AIRFOIL is used to compute the sound radiated from a single airfoil due to those mechanisms related to the airfoil wake turbulence. A development of the model was presented in detail in Volume 1 of this report. Through the model, the sound radiation is related to the turbulent structure in the wake of the airfoil.

The equation which forms the basic result of the model and that programmed here is

$$G_{\rho}(\vec{x},\omega) = \sum_{i=1}^{2} \sum_{j=1}^{2} 16 \text{ S } L_{1}^{2}(u_{i}u_{j},\omega) L_{2}(u_{i}u_{j},\omega) L_{3}(u_{i}u_{j},\omega)$$

$$\omega^{4} \int_{y_{2}} A_{\underline{i}} A_{\underline{j}} \overline{u_{\underline{i}} u_{\underline{j}}} (y_{2}, \omega) dy_{2}$$

with:  $A_1 = \rho_0 U_1 \sin \psi / (4\pi a_0^3 | \overline{x}^{\dagger})$ 

$$A_2 = \rho_o \overline{U}_1 \cos \psi / (4\pi a_o^3 |\hat{\mathbf{x}}|) .$$

I menclature used here is the same as that of Volume 1.

The integration noted above is performed using a Lagrangian method. This subroutine is part of the University of Washington Computer Library. Any simple numerical integration scheme may be substituted for this subroutine. In the program the subroutine is labeled LAGRAN.

#### 2.1 Program Input

AIRFOIL is a simple computational program. It consists of three subprograms. The main program is AIRFOIL in which the actual computations are made. The next is subroutine DREAD in which data are read into and conditioned to form the variables used in the actual computations. Finally, DWRITE in which the results of the computations are written out.

Input to the program is accomplished using IBM cards. In the following we will list each card type, the variable names and their descriptions.

### CARD 1, FORMAT (7F10.2)

PATM	atmospher c static pressure	(atm)
TATM	" temperature	(°C)
SPAN	airfoil ength	(cm)
XLAM	length in the stream direction (this is a dead variable in the current program so any input is okay	(cm)
DEL	wake thickness	(cm)
RAD	distance from airfoil to sound observer	(m)

#### CARD 2, FORMAT (215)

NPF number of frequency points where data will be input

NPY number of positions in the wake where data will be given

#### CARD 3, FORMAT (7F10.2)

Y(I) positions in the wake measured relative to I = 1,NPY the wake centerline (cm)

Note that if more than 7 entries are needed, additional cards will be required for this variable.

#### CARD 4, FORMAT (7F10.2)

FREQ(I)	frequencies at which the following correlation lengths are to correspond	(Hz)

XL(I) correlation length in stream direction for the longitudinal turbulent component (cm) YL(I) correlation length across the wake for the longitudinal turbulence component (cm)

correlation length in the span direction ZL(I) for the longitudinal turbulence component (cm)

# CARD 5, FORMAT (7F10.2)

same as for CARD 4 FREQ(I)

same as for CARD 4, but for the transverse XI(I)(cm) turbulence component

same as for CARD 4, but for the transverse YT(I) (cm) turbulence component

same as for CARD 4, but for the transverse ZT(I) (cm) turbulence component

Notice that CARD's 4 and 5 are read inside a DO loop. The statements are

DO 16 I = 1,NPFREAD(5,3) FREQ(I),XL(I),YL(I),ZL(I)16 READ(5,3) FREQ(I), XT(I), YT(I), ZT(I)

Certainly more than just the two cards will be required here since more than one spectral point will generally be required. For this outline, we will continue with CARD 6 keeping in mind that CARD 6 refers to a new input type of data rather than the actual number of the card in the input file.

#### CARD 6, FORMAT (7F10.2)

ratio of wake velocity at Y(I) to the velocity XI(I)(--) in the free stream UMEAN 1 = 1,NPY

#### CARD 7, FORMAT (7F10.2)

ratio of spectral level at FREQ(I) to the RMS DDB1(I) level; this is for the longitudinal component 1 = 1,NPF (dB) of turbulence

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DDB1 can be interpreted from the equation for its usage which is

$$u_1'(f) = u_1^2 * 10. **(-DDB1(I)/10.)$$

 $u_1^{\prime}(f)$  is the actual spectral level sought, and  $u_1^2$  is the RMS level for the longitudinal component of turbulence.

CARD 8, FORMAT (7F10.2)

DDB2(I) the ratio of the spectral level at FREQ(I)

I = 1,NPF to the RMS level for the shear component of turbulence (dB)

see the note for DDB1

CARD 9, FORMAT (7F10.2)

DDB3(I) the ratio of the spectral level at FREQ(I) to the RMS level for the transverse component of turbulence (dB)

CARD 10, FORMAT (7F10.2)

Ull(I) spatial distribution of the RMS level of I = 1, UPY longitudinal turbulence across the wake, normalized with UMEAN

CARD 11, FORMAT (7F10.2)

U11(I) spatial distribution of the RMS level of the shear stress across the wake, normalized with UMEAN

CARD 12, FORMAT (7F10.2)

U22(I) spatial distribution of the RMS level of the transverse turbulence across the wake, normalized with UMEAN

This completes the inpat for the program.

Program output consists of a listing of the input variables and of the spectral distribution of the radiated sound pressure at each radiation angle  $0^{\circ}$  through  $180^{\circ}$  in  $10^{\circ}$  increments. The radiated sound is presented in dB by normalizing the pressure with a reference  $20\mu N/m^2$ .

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# 2.2 Program Listing

```
PROGRAM AIRFOIL (INPUT, OUTPUT, TAPES=INPUT, TAPE6=UUTPUT)
      THIS PROGRAM COMPUTES THE SPECTRUM OF RADIATED SOUND FROM
      CORRELATION AND SPECTRAL DATA GIVEN FOR TWO POINT VELOCITY
      CORRELATIONS IN THE WAKE OF A SINGLE AIRFOIL
      DIMENSION XINTG(11) XINT1(11) XINT(11)
      DIMENSION FREG(20), XL(20), YL(20), LL(20), 0101(11,20), X1(11)
     101U2(11,2U),U2U2(11,2U),Y(11),Xm(11),XUmEG(2U),
     2P5D(20), SPL(20), VCL(20), VCL(20), VAR(3), X1(20)
      DATA P1/3.14159/
     READ IN DATA .
C
      PATM = STATIC PRESSURE (MM HG)
C
     TATM = STATIC TEMPERATURE (DEG C)
CC
       SPAN = AIRFOIL LENGTH (CM)
C
      XLAM = STREAM INTEGRATION LENGTH (CM)
      DEL = WAKE THICKNESS (CM)
C
      UMEAN = FREE STREAM VELOCITY (M/SEC)
C
     RAD = DISTANCE TO OBSERVER (M)
      NPF = NUMBER OF FREQUENCY POINTS IN SPECTRUM
      NPY = NUMBER OF SPATIAL POINTS IN WAKE
      Y = LOCATIONS OF THE POINTS IN THE WAKE (CM)
C
      FREQ = FREQUENCY ARRAY (HZ)
      XL = STREAM CORRELATION FOR UIU1 (CM)
C
      YL = CORRELATION ACROSS THE WAKE FOR UTUL (CM)
      ZL = SPAN CORRELATION FOR UIUI (Cm)
C
      XT = STREAM CORRELATION FOR U2U2 (CM)
Ç
      YT = CORR-LATION ACROSS THE WAKE FOR U2U2 (CM)
      ZT = SPAN CORRELATION FOR U2U2 (Cm)
      XI = RATIO OF WAKE VELOCITY TO UMEAN
Ċ
      DDB1 = RATIO OF SPECTRAL LEVEL TO KMS - U101 (DB)
Ċ
      DUBZ = RALIO OF SPECTRAL LEVEL TO RMS - UIU2 (DB)
Ċ
      DUD3 = RATTO OF SPECTRAL LEVEL TO KMS - U2U2 (DD)
Ċ
      Ull = RMS VALUE OF UlU1 (PERCENT)
C
      U12 = RMS VALUE OF U1U2 (PERCENT)
      U22 = RMS VALUE OF U2U2 (PERCENT)
      CALL DREAD! AO PRHO PI BM NOMEGO VCL VCT SPAN NILAM DEL XMO
     1RAU > U1U1 > U1U2 > U2U2 > NPF > NPA > NPT > X > Y > FREW > PATM > TALM > XL > XT)
      COMPUTE RADIATION PATTERN
      COEF1=(RHO/(4.*PI*RAD))**2
      COEF2=COEF1*SPAN*BM**2
      DO 2000 KK=1,19
      UKK=KK
      CODE1=UKK
      THETA=-90.+10.*(UKK-1.)
      THET=THETA*PI/180.
      ST=5IN(THET)
      CT=COS(THET)
      5T5=5T**2
      CTS=CT**2
      STCT=ST*CT
```

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```
COEF3=COEF2
      COMPUTE SPECTRUM
      DO 1000 K=1,NPF
      COMPUTE INTEGRALS OVER THE WAKE VOLUME
      XINT(K)=U.U
      DO 300 II=1.3
      DO 100 I=1 NPY
      VAR(1)=ST3*U1U1(K,1)**2*VCL(K)*XL(K)
      VAR(2)=STCT#U1U2(K,I)**2*(VCL(K)+VCT(K))/2.**(XL(K)+XT(K))/2.
      VAR(3)=CTO*U2U2(K,I)**2*VCT(K)*XT(K)
  100 XINTG(I)=VAR(II)
      wRITE(6.10) (XINTG(I):I=I:NPY)
   10 FORMAT(7E1J.2)
      CALL LAGRAN(Y , XINTG , NPY , 1 , 1 , U , ANG , I KRUK)
  300 XINT(K)=ANS+XINT(K)
      PSD(K)=XINT(K)*COFF3*XOMEG**4
      PSD(K) = ABS(PSD(K))
      WRITE(6,11) ANS
   11 FORMAT(4H ANS
                       1E2(.5)
 1000 SPL(K)=10.*ALUG1U(PSD(K)/400.E-12)
      CALL DWRITE (AUSRHOSPISBMSXUMEGSVCLSVCTSSPANSXLAMSDELS
     1XM+KAD+U1U1+U1U2+U2U2+X+Y+FHETA+PSD+SPL+NPY+NPX+NPF+
     2FREQ, CODE1, PATM, TATM, XL, XT)
 2000 CONTINUE
      3TOP
      END
      SUBROUTINE DREAD (AO+KHU+PI+BM+XUMEG+VCL+VCT+SPAN+XLAM+DEL+XM+
     IRAD DUIUI DUIU2 DU2 DA PERNEKAN NEKANAN KANAN TARIN TARIN XL DXI)
C
      THIS SUBROUTINE READS AND CONDITIONS INPUT DATA
      DIMENSION FREQ(20), XL(20), YL(20), ZL(20), JU101(11,20), XI(11),
     IUIU2(1192V);U2U2(1192U);Y(EI);XM(II);XUMEG(2U);
     2 PSD(20) + SPL(20) + VCL(20) + VCI(20)
      DIMENSION DDB1(20),DDB2(20),DDB3(20),U11(11),U12(11),
     1022(11),DF1(20),DF2(20),DF3(20),X7(20),YT(20),Z1(20)
      DATA CR, Cu, GAM/288., 1.0,1.4/
      READ(5.1) PATM.TATM.SPAN.XLAM.DEL.UMEAN.RAD
    1 FORMAT(7F10.2)
      CMFT = .0328
      PATM = 2116.*PATM
      TATM=(TATM+32+)*9-/5++460-
      SPAN=SPAN*CMFT
      XLAM=XLAM*CMFT
      DEL=DEL*CMFT
      UMEAN = UMEAN*CMFT*100.
      RAD = RAD*CMFT*100.
```

```
DSCALE=1.0
   AO=SORT (GAM*CR*CG*TATM)
   RHU=PATM/(CG*CR*TATM)
   BM=UMEAN / AC
   READ(5,2)
              NPF, NPY
 2 FORMAT(315)
   READ(5:1)
               (Y(I) \rightarrow I = I \rightarrow NPY)
   DO 18 I=1 NPY
18 Y(I) = CMFT*Y(I)
   DO 16 I=1 NPF
   READ(5,3) FREW(I), XL(I), YL(I), 4L(I)
16 REAU(5.3) FREQ(I) XT(I) YT(I) 4T(I)
   DO 10 K=1 NPF
   XOMEG(K)=Z.*PI*FRFQ(K)
   FREQ(K)=FREQ(K)/USCALE
   XUMEG(K)=XUMEG(K)/DSCALE
   CUEF=2./(4.54*12.)
   XL(K) = XL(K) *COEF
   YL(K) = YL(K) * COEF
   ZL(K) = ZL(K) *CUEF
   XT(K)=XT(K)*COEF
   YT(K)=YT(K)*COEF
   ZT(K) = ZT(K) * COEF
   VCL(K) = XL(K) * YL(K) * XL(K)
TO VCT(K) = XT(K) *YT(K) *AT(K)
   READ(5.1)
               (XI(I),I=1,NPY).
   DU 13 I=1:NPY
13 XM(I)=UMEAN*XI(I)/AO
   READ(5 + 1) (DDB1(K) + K = 1 + NPF)
   KEAD(5.1) (DUB2(K) K=1.NMF)
   READ(5,1) (DD83(K),K=1,NPF)
   DO 12 K=1,NPF
   DF1(K)=10.4*(-DDB1(K)/20.)
   DF2(K)=10.4*(-DDB2(K)/20.)
12 DF3(K)=10.**(-DDB3(K)/20.)
   READ(5)1) (011(1))1=1>NPY)
   READ(5,1) (U12(I),I=1,NPY)
   READ(5.1)
               \{U22\{I\},I=1,NPY\}
   DO 15 K=I NPF
   DO 15 I=1 NPY
   U1U1(K,I)=DF1(K)*U11(I)
   U1U2(K) I)=DF2(K)*U12(I)
15 U2U2(K,1)=DF3(K)*U22(I)
 3 FORMAT(4F1-2)
   RETURN
   END:
   SUBROUTINE DWRITE (AUSRHUSPISEMSXUMEGSVCLSVCTSSPANSXLAMSDELSXMSRADS
  101019U1U29U2UZ9K9Y:THETA:PSD:SPL:NPY:NPX:NPF:FKEW:CUDE1:
  2PATM . TATM . XL . XT)
```

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```
DIMENSION FREQ(20), XE(20), YE(20), 4E(20), 5U101(11,20), XI(11),
  10102(11,20),0202(11,20),Y(11),XM(11),XMEG(20),
  2 PSD(20), SPE(20), VCE(20), VCT(20)
   IF(CODE1.GT.1.) GO TO 21
   WRITE(6:1)
 1 FORMAT(1H1,80H SOUND RADIALION FROM A SINGLE ALREGIL AS RELATED TO
  IWAKE AERODYNAMIC PARAMETERS
                                 111
   WRITE(6,2) PATM + TATM + SPAN + XLAM + DEL + KAD
 2 FORMAT(17H AMBIENT PRESSURE 1F10.2.2.2.H AMBIENT TEMPERATURE
  11F10.2//29H DIMENSIONS OF INTEGRALION /13H AIRFOIL SPAN
  21E20.5,10X.17H STREAM DIRECTION 1E20.5/15H WAKE THICKNESS
  31L20.5//19. RADIUS TO OBSERVER 1620.2///)
   wRITE(6,3) (Y(I),I=1,NPY)
 3 FORMAT(3UD STEADY FLOW MACH NUMBER FIELD/1/D STREAM DIRECTION
  130X = 16H ACKUSS THE WAKE /20X = 10F10 = 4/)
   WRITE(6,4) (XM(I),I=1,NYY)
 4 FURMAT(5X, 1F10.4, 5X, 10F10.5)
   DO 20 K=1 *NPF
   wRIIE(6.6) FREQ(K). vCL(K). vCI(K)
 6 FURMAT(IHI) 10H FREQUENCY
                              1EZU.5:19H CURR VULUME (LUNG) 1EZU.5:
  119h CORR VOLUME (TRAN) 1E20.5//)
   WKI[E(6,7) (Y(I),I=1,NPY)]
 7 FORMAT(34H LONGITUNINAL TURBULENCE COMPONENT //17H STREAM DIRECTIO
       SUX, IOH ACROSS THE WAKE/ZUX, TUFTU.Z/)
  1N
   wRITE(6,4) (UIUI(K,I), I=1,NPY)
   wXIIE(6.8) (Y(I), I=1.NPY)
 8 FORMAT(//ozh TRANSVEKSE TURBULENCE COMPONENT//17H STKEAM DIRECTION
  13UX + 16H ACROSS THE WAKE /2UX + LUFTU - 2)
   wRITE(6,4) (U2U2(K,I),I=1,NHY)
   wRITE(6,9) (Y(I),I=I,NPY)
 9 FORMATI//27H SHEAR TURBULLINGE COMPONENT //17H STREAM DIRECTION
  130X,16H ACROSS THE WAKE /20X,10F10.2/1
   WRITE(6,4) (U1U2(K,1),I=1,NPY)
20 CONTINUE
21 CONTINUE
   wRITE(6,11) THE A
11 FORMAT(1H1,25H PREDICTED SOUND SPECTRUM //16H RADIATION ANGLE
  11F10.2//IOH FREWUENCY 1UX:17H KADIATED SPL(DB)
   DO 12 I=1.NPF
12 WRITE(6,13) FREG(I), SPL(I)
13 FORMAT (1F10,2,10X,1F10,2)
```

RETURN END

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#### 3.0 PROGRAM ROTOR

The purpose of developing program ROTOR was to provide a method for the prediction of sound generation from turbomachinery rotors. Aerodynamic operation was limited to the subsonic flow regime. Both tone noise and broad band effects were included. The tone noise part of the model was simply the steady state forces on the rotor blades. The broad band mechanism was taken as the force fluctuations which were relatable to the wake turbulence of the individual airfoils of the rotor. The mathematical model used for the basis of the sound radiation was that presented by Ffowcs Williams and Hawkings.

To use the program one must supply the aerodynamic parameters for the particular design. Program ROTOR then computes the spectrum of sound radiated by the machine due to the mechanisms noted above.

The program is divided into five subroutines. A brief discussion of the contents of these subroutines will be given to provide some familiarization with the program structure. The names of the subroutines are:

DATAIN, WAKE, ORTH1, TGNE, and ORTH2..

#### 3.1 Subroutine DATAIN

As the name implies, DATAIN is used to read and condition the input data. The data input can be listed with the required FORMAT and physical units. The following are the only inputs required to run the program.

#### CARD 1, FORMAT (7F10.2)

RPM	rotor speed	(RE	М)

R1 distance to observer (M)

<sup>&</sup>quot;Theory Relating to the Noise of Rotating Machinery," J. Sound if Vib., 10, 1, 1969.

	В	number of rotor blades	(-)
	Ul	blade relative velocity	(M/SEC)
	XLAM	blade stagger angle	(DEGREES)
	RS	source radius	(M)
	FMAX	maximum frequency in spectrum	(IIZ)
CARD	2, FORMAT (7F	10.2)	
	FB	magnitude of force on each blade	(kg)
•	Ululb	RMS turbulence level for the longitu- dinal component, normalized with Ul	()
	U1U2B	RMS shear turbulence, normalized with Ul	()
	U2U1B	RMS shear turbulence, normalized with U1	()
	<b>U2U2</b> B	RMS turbulence level for the transverse component, normalized with U1	()
CARD	3, FORMAT(7F	10.2)	
	ZL	blade span or other span length used to define the length of the source in the span direction	(M)
	YL	thickness of the airfoil wake	(M)
CARD	4, FORMAT(11	5)	
	NF	number of frequency points to be used to input random data for wake related sound generation	()

In the remaining inputs a FORMAT(7F10.2) is used but if more than NF = 7 is used then more than one card will be needed for each of the input variables. Here we will list the variable arrays as if only one card will be required for the input.

# ALL FOLLOWING CARDS, FORMAT (7F10.2)

F(I)	array of frequency values	(HZ)
CORR(I)	an arbitrary spectral shaping factor, normally set equal to 1	()
XLL(I)	correlation length in the stream direction, based upon the longitudinal component of turbulence	(CM)
YLL(I)	correlation length in the direction across the wake, based upon the longitudinal component of turbulence	(CM)
ZLL(I)	correlation length in the span direction, based upon the longitudinal component of turbulence	(CM)
XLT(I)	correlation length in the stream direction, based upon the transverse component of turbulence	(CM)
YLT(I)	correlation length in the direction across the wake, based upon the transverse com- ponent of turbulence	(CM)
ZLT(I)	correlation length in the span direction, based upon the transverse component of turbulence	(CM)

The following variables, U1U1, U1U2, U2U1, and U2U2, are spectral levels given in dB relative to the RMS levels for the component. The result of this procedure will be: if these turbulence quantities are given in dB down from RMS on a 1/3 octave spectrum then the radiated sound will also be 1/3 octave. If 6% spectra are used then the radiated sound will be 6%, also.

U1U1(I)	longitudinal component of turbulence	(dB)
U1U2(I)	shear stress component	(dB)
U2U1(I)	shear stress component	(dB)
112112 (I)	transverse component of turbulence	(dB)

All input data are printed out in the physical units used in the computations.

#### 3.2 Subroutine WAKE

This subroutine computes the wake related sound generation by the rotor. The model used to relate the force fluctuations on the rotor blading to aerodynamic variables is the single airfoil model. The expression which results and is here computed is

$$\left| p(\vec{x}, \omega) \right|^2 = \frac{1}{16\pi^2 r^2} \sum_{n=-\infty}^{\infty} \sum_{k=1}^{B} \left( \frac{\omega}{a_0} \right)^2$$

$$d_r(\theta_k, f-n\Omega) d_r^*(\theta_k, f-n\Omega) J_n^2(\frac{-\omega R_s \sin \phi}{a_o})$$
.

For the present case, the force fluctuations are

$$\begin{split} \mathbf{d}_{\mathbf{r}}(\boldsymbol{\theta}_{k}, & \text{f-}\boldsymbol{n}\Omega) & \mathbf{d}_{\mathbf{r}}^{\star}(\boldsymbol{\theta}_{k}, & \text{f-}\boldsymbol{n}\Omega) = S \, \delta_{\omega} \, \left(\omega - 2\pi\boldsymbol{n}\Omega\right)^{2} \, \rho_{o}^{2} \\ & \sum_{\ell=1}^{3} \, \sum_{m=1}^{3} \, \hat{\boldsymbol{\tau}}_{\ell} \hat{\boldsymbol{\tau}}_{m}^{\star} \, \, 16 \, \, L_{1}^{2}(\boldsymbol{u}_{\ell}\boldsymbol{u}_{m}, \omega) \, \, L_{2}(\boldsymbol{u}_{\ell}, \boldsymbol{u}_{m}, \omega) \, \, L_{3}(\boldsymbol{u}_{\ell}, \boldsymbol{u}_{m}, \omega) \, \, \boldsymbol{u}_{\ell} \boldsymbol{u}_{m}^{\star}(\omega) \, . \end{split}$$

where: S = span,  $\delta_w = \text{wake thickness}$ ,  $L_i = \text{correlation lengths}$  (i = 1,3),  $\overline{u_1 u_m} = \text{spectral level of turbulent stress}$ ,  $\omega = \text{radian frequency}$ ,  $\Omega = \text{rotor speed}$ , and f = frequency in Hz.  $J_n$  is a Bessel function of the first kind of integer order.

The output from this subroutine is the radiated sound pressure level expressed in dB relative to a reference pressure of 20  $\mu N/m^2$ .

#### 3.3 Subroutine ORTH1

This subroutine computes the components of the position vector of the sound observer in the coordinate system relative to each of the rotor blades.

The product of these components with the force components on the blades yields the force in the direction of the observer. To do this the position vector must first be expressed in terms of the rotor coordinate system. It must then be rotated by the blade stagger angle to be in the blade coordinate system.

The observer position vector components for a typical blade now may be written:

$$r_{1} = (r \sin \phi - R_{s} \cos \theta)/[r(1 - \frac{R_{s}}{r} \sin \phi \cos \theta)]$$

$$r_{2} = -\frac{R_{s}}{s} \sin \theta/[r(1 - \frac{R_{s}}{r} \sin \phi \cos \theta)]$$

$$r_{3} = \cos \phi/(1 - \frac{R_{s}}{r} \sin \phi \cos \theta)$$

The change from the observer coordinates to those of the rotor blade can be expressed in the rotation

$$\begin{pmatrix} -\sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \\ \cos\theta & \sin\theta & 0 \end{pmatrix}$$

and the further rotation by the stagger angle,  $\lambda$ ,

$$\begin{pmatrix} \sin \lambda & \cos \lambda & 0 \\ -\cos \lambda & \sin \lambda & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

The stagger angle,  $\lambda$ , is the angle between the airfoil chord and a radial plane passing through the axis of the rotor.

#### 3.4 Subroutine TONE

Subroutine TONE as currently set up computes the sound generation related to the steady state blade forces. This is the "Gutin" mechanism. The program has been developed for a rotating steady state stress term also but as yet it is not known how to model this in terms of aerodynamic design parameters.

The expression which is computed for the radiated sound pressure is

$$|p(\hat{\mathbf{x}},\omega)|^2 = \frac{1}{16\pi^2r^2} \left(\frac{B}{R_s}\right)^2 \sum_{k=1}^{B} \sum_{m=-\infty}^{\infty} m^2 F_r^2 \left(\theta_k,\omega\right) J_{mB}^2 \left(\frac{\omega R_s \sin \phi}{a_o}\right)$$

where: B = number of blades in the rotor

 $F_{\mu}$  = blade force in the direction of the observer

R = source of radius

 $\phi$  = observer angle to rotor axis

r = distance to the observer

ω = radian frequency

#### 3.5 Subroutine ORTH2

ORTH2 does exactly the same computation to the blade force as ORTH1 did for the random blade forces. The procedures are parallel.

```
PROGRAM ROTOK(INPUT)OUTPOLITAPES=INPULITAPE6=GUTPOT)
      ALROPYNAMIC SCUND GRNERALION FROM MULTIDLAULD RUTORS
      ... THE RAPIATED SOUND SPECTROM IS PREDICTED BASED
         ON STEADY LOADS AND AIRHOIL WAKE STATISTICAL PROPERTIES...
      DIMENSION 0101(50),0102(50),0201(50),0202(50),F(50),F(200),
     1KHOT(200)*KHOa(30)*CORK(30)*XLE(30)*XET(50)*VCE(30)*VCF(30)
Ĺ.
      CALL THE PUBROULING TO INPUT AND CONDITION THE DATA
      CALL DATAIN (ULUISUI UZ SUZUI SUZUZ SF SKPOSKI SBSUI SALAMSKOSF MAKSFESMF S
     12L, YL, XLL, XLT, VCL, VC[, CURK)
      1K1 + XLAM + U1 + ZL + YL + XLL + XLT + VCL + VCT + CONN)
C
      WAKE COMPUTES BRUAD BAND SOUND SENERATION
      CALL TONE(RISESPES PRO ISALAMSKY) SRUSULSTI
      TONE COMPOTES LEVEES OF PORE TONE DENERATED BY MOTATING
      STEADY BEADE FORCE AND MEAN VALUES OF STRESS TENSOR
      5TJP
      CHEMAJA CLOCACINC DACATE TO SUCCESSIVE SULVES ALANDOS
     IFMAX, FB, NF, SZL, SYL, SZLL, SZLI, SVCL, SVCL, SCURK)
Ć
      READS AND CONDITIONS DATA
      DIMER ION U101(50) + U102(50) + U201(50) + U202(50) + F(50)
      DIMENSION VC(30), CORR(30), XLL(30), YLL(30), 4LL(30),
     2XLT(3U) +Y=1(3U) +/LT(3U) +VC1(3U) +VCL(3U)
C
      RPM = ROTUR SPELD (RPM)
      RI = ObockVER RADIOS (所)
      L = NOMBER OF ROLER BLADES
      OI = DEADE RELATIVE VELOCITY (M/SEC)
      XLAM = STAGGER ANGLE - MEASURED FROM FAN AXIS (DEG)
C
      RS = SOURCE RADIUS (m)
C
      FMAX = MAXIMUM FX#QUENCY OF INTEREST (HZ)
C
      Fo = blade FORCE (KG)
      JIDIB = RAS LONGITUDINAL TURBULENCE - NURMALIZED WITH UI
C
      ULUZO = RMS SMEAK - NORMALIZED WITH UT
C
      UZUID = RMS SHEAR - NORMALIZED WITH UI
C
      0202B = RMS TRANSVERSE TORBULENCE - MORMALIZED "I'IN 01
C
      ZL = SPAN DIMENSION (CM)
C
      ZL = WAKE THICKNESS (CM)
C
      CHD = BLADE CHORD (CM)
      NF = NUMBER OF FREQUENCY POINTS
Ç
      F(I) = FREQUENCY ARRAY (HZ)
      CORR(I) = A SPECIRAL WEIGHTING FUNCTION (NORMALLY UNITY)
Ĺ
C
      XLL(I) = STREAM CORRELATION LENGTH FOR Ulula
Ć
      YLL(1) = NORMAL CORRELATION LENGTH FOR GIULD (CM)
C
      ZLL(1) = 5PAN CORRELATION LENGTH FOR GIOLS (CM)
C
      ∠LI((I) = ⇒TREAM CORRELATION LENGTH FOR U2U2B ((I))
C
      YLT(I) = NORMAL CORRELATION LENGTH FOR U2U2
C
      ZLT(I) = SPAN CORRELATION LENGTH FOR S202 (CM)
```

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```
C
                                          (RMS)
      Ulul(I) = DB DOWN FROM Ululb
C
      Uluz(I) = DB DOWN FRUM UluzB
                                         しいがい)
C
      U2U1(I) = DB DOWN FROM UZU1B
                                         (KMO)
C
      U2U2(I) = DB DOWN FROM U2U2B
                                         (KMS)
      DATA AO, Co, PI/342, , 1.0, 3.14109/
      READ(bol) RPMoRloBouloXLAmoRDoFMAX
      READ(りょ上) FosululBsulu ロチンといエロチリ2いとロ
      KEAD(5,1)
                    ZL, YL, XL, CHD
      CHF = .0328
      RI=RI*CMFT*100.
      U1=U1*CMFT*100.
      KS=RS*CMFT*100.
      FB=FB*2.21
      ZL=ZL*CMF1
       Y L = Y L * C MF T
      CHD=CHD*CMFT
    1 FORMAT(7Fiu.2)
      TPI=2.*PI
      XLA = XLA = * PI/18 J.
      RPS=TPI*RHM/60.
      READ(5:2) NF
    2 FORMAT(115)
      READ(5,1)
                   (F(I) * I = 1 * Nf)
      KEAD(5,1)
                   \{CGRK(I), I=1, NF\}
                   (XLL(1), I=1,NF)
      REAU(5,1)
      KEAD(5:1)
                   (YLL(I), I=1,NF)
      READ(5,1)
                   \{\angle LL\{[j], [=], NF\}
      READ(5:1)
                   (X L I (I), I=1, NF)
                   (YLT(I) \bullet I = 1 \bullet NF)
      READ(5:1)
                   (ZLT(I),I=1,NF)
      READ(5:1)
                   (U]U](T) = [ = 1 = NF)
      READ(5:1)
      KEAU(5,1)
                   (U1U2(1), I=1,NF)
                   (\cup 2\cup 1)(I) \circ I = 1 \circ NF
      READ(5:1)
                   (U2U2(I), I=1,NF)
      READ(5:1)
C
       INTRODUCE SCALING FACTORS
      oCL=(CHD/3.0)**∪.8*(U1/15∪.)**(-U.2)
       oCF=(U1/100.)**1.2*(CHD/3.0)**(-0.8)
      FMAX=FMAX*JCF
       メレニメドックト
       YL=YL*oCL
      ZL=ZL*SCL
      DO 30 I=1.NF
      F(I)=F(I)*5CF
      XLL([)=XLL([)*SCL
      YLL(I)=YLL(I)*SCL
      ZLL(I)=ZLL(I)*5CL
      XLI(I)=XL+(I)*SCL
       YLI(I)=YLT(I)*SCL
   30 ZLT(I)=ZL1(I)*SCL
      DO 20 I=1 NF
       VCL(I)=8.*XLL(I)*YLL(I)*4LL(1)/28350.
   20 VCT(I)=8.*XLT(I)*YLT(I)*4LT(1:/28350.
```

```
C
      WRITE TIE INPUT DATA
      wRIIc(6,3)R1,RPm,FB,ALAM,B,R0,01,FmAX,0101B,0102B,0201B,0202B
    3 FORMAT(IHI: 54h AEROUYNAMIC SOUND OLNERATION FROM MOLTIDLADED ROTOR
     15//23H OBSERVER DISTANCE (M)
                                      1F7.2.10X.12H ROJOR SPEED
     21F10=2/19m STEADY BEADE FORCE 1F11=291UX,20m DLADE STAGGER ANGLE
     31F10+2/17H, NUMBER OF BLADES 183+4,20%,14H SOURCE RADIUS
     HIFO.Z/ZHH DLADE RELATIVE VELUCITY IFO.ISIOASION MAX. FREQUENCY
     51F10.2/10H U1U1(KM5) | lEiv.3)2A:lon U1U2(RM3) | leiv.3)5A;
     610H J2U1(Km5) 1E10.3,5X,1JH J2UZ(Km5) 1E10.3////)
      WRITE(6,9) ZL,YL
    9 FORMAT(21H WAKE VOLUME L(Z) =
                                        1E15.5.5X.
     18H L(Y) = 1615.5//)
      WRITE(6,11)
                                                                   F(X)
   11 FORMAT(100H
                      FREQUENCY
                                             L(Z)
                                     JUALR FACTOR
                  L(X)
      WRLIE(6,1c) = (F(1), cll(I), Yll(I), Xll(I), clur(I), l=1, NF)
      wRITL(6,14) = (f(1),2LI(1),3LLI(1),3LLI(1),3CURR(1),i=1,NF)
   12 FORMAT(5EZU-5)
      WRITE(6,4)
    4 FORMAT(14H SPECTRUM U1U1 //)
      wRITE(6,5) (F(I),U1\cup I(I),I=1,NF)
    5 FORMAT(4(1F10.3:1E20.4))
      WRITE(6,6)
    6 FURMATITITIES SPECTRUM U102 1/1
      wRITE(6.5) = (F(1).U1U2(1).I=1.NF)
      WRITE(6,7)
    7 FORMAT(///14H SPECTRUM 0201 //)
      MRIIE(6,5) (F(1),U2UI(I),I=1,NF)
      WRITE(6.8)
    8 FORMAT(///14H SPECTRUM U2U2 //)
      WRITE(6.5) (F(I).02-2(I).1=1.NF)
C
      CONVILION TORBULLNCE DATA TO LINEAR SCALE
      DO 10 I=1 NF
      XLL(I)=XLL(I)/(2.54*12.)
      XLT(I) = XLI(I)/(2.54*12.)
      Ulu1(1)=U1U1B/(1U.**(U1U1(1)/2U.))
      U1U2(1)=U1U2B/(1U_***(U1UZ(1)/2U_*))
      U2U1(1)=U2U1d/(10.**(d2U1(1)/20.))
   10 U2U2(I)=J2U2B/(10.**(U2U2(I)/20.))
      RETURN
      END
      JUBRUUTINE WAKE(F, U101, 0102, 0201, 0202, NF, RPJ, FMAK, KS, KHUJ, B,
     1K1 + XLAM: • U1 + ZL + YL + XLL + XLT + VCL + VCT + CUKK)
C
      COMPUTES SOUND RADIATION FROM WAKE TORBOLENCE PROPERTIES
      DIMENSION F(30):01U1(30):01Oz(30):02O1(30):02O2(30):BE5(10O0):
     1BEN(1000) *PHI(20) *SX(30 *3) *51 (30) *
     2RHU5(30), V1(3), VC(30), CUKR(30);
     3XLL(30),XLT(30),VCL(30),VCT(30)
```

DATA CG. AO. Pl. RHO/1.0.342.43.14159.1.175/

```
PREF=20.E-06/A0**2
      PREF=PREF*PREF
      C1=1./(4.*PI*AO**2*R1)**2
      TPI=2 *PI
      C2=C1*(RH0/CG)**2
      REV=RPS/TPI
      A TOT = ZL*YL
C
      COMPUTE THE RADIATION RATTERN
      DO 1000 KK=1,3
      PHI(KK)=45.*FLOAT(KK-1)
      PHIP=PHI( \( \Lambda \) *PI/180.
C
      COMPUTE THE SPECTRUM
      00 11 I=1 NF
      DVL=VCL(I) #ATUT #CORK(I)
      DVI=VCT(I)*ATOT*CORK(I)
      DVL=5QRT(DVL)
      DVT=SQRT(DVT)
      DV=0.0
      \supset X(I > 1) = -\cup 1 \cup I(I) * D V L * \supset QR | (XLL | I))
      3X([,2]=0202([)*DVT*3@k[(XL[([))
      JU 40 J=1+3
   40 wkITt(6,41) 5X(I,J)
   41 FORMAT(10H SX([,J) =
                                 1E2v•5)
      DO 32 J=1.3
   32 VI(J)=5X(I,J)
      V3=U1U2(I)
      V4=U2U1(I)
      FRA=F(I)*IPI
      CALL ORTHI (VI + FKA + V3 + V4 + PHIP + ALAM+ B + Kl + N3 + DD)
   11 51(I)=DD
      DO 2000 K=1,NF
      C3=(TPI*F(K)/AO)**2*U1**2
C
      THE ARGUEMENT FUR THE BESSEL FUNCTION
      ARG=-TPI*r(K)*Ro*SIN(PHIP)/AG
C
      NAME IS THE MAXIMUM NECESSARY VALUES OF N FOR THE DESSEL FUNCTION
      N-AX=IFIX(FMAX*TPI/RPS)*2+1
      NMAX=250
      IF (NMAX.GI.400) NMAX=400
      IF (ARU.NE.U.U) GO TO 60
      BE5(1)=1.0
      DU 61 LL=2 NMAX
   61 BES(LL)=0.0
      GO TO 62
                                      REPRODUCIBILITY OF THE
   60 CONTINUE
                                       ORIGINAL PAGE IS POOR
      DO 63 LL=1.NMAX
```

```
63 BES(LL)=U.U
      CALL NBESU (ARG, NMAX, BES)
   62 CONTINUE
      SQUARE THE BESSEL FUNCTIONS
C
      DO 44 J=1*NMAX
      BEN(J)=(-1.)**(J-1)*BES(J)
      BEJ(J)=BEJ(J)*BEJ(J)
   44 BEN(J;=BEN(J)*BEN(J)
C
      PROVIDE THE SUMMANDS
      5UM1=0.0
      DO 14 N=1 NMAX
      FP=F(K)+FLOAT(N-1)*KLV
      IF(FP.GT.FMAX) GO TO 13
      Doml=[BLU1(FP,F,u1,1)NF)
      DUM1=DUM1*(TPI*FP)**2
      GO TO 14
  13 DUM1=0.0
   14 SUM1=SUM1+DUM1*BES(N)
      DO 12 N=2 NAX
      FN=F(K)-FLOAT(N-1)*RLV
      IF(FN.LT.-FBAX) GO 10 15
      FN=AB5(FN)
      Duml= | BLul (FN + F + 51 + 1 + NF)
      DUM1=DUM1*(TPI*FN)**2
      GO TO 12
   15 DUM1=0.0
   12 SUM1=SUM1+DUM1*BEN(N)
      WRITE(6,31) 50M1,DUMI
   31 FORMAT(5H SUM1 1E20.5.5) DUML 1E20.5)
C
      THIS COMPLETES THE DIPOLE LERM
      WRITE THE MODULUS OF THE RADIATED SOUND DENSITY
C
      VARI=C2*C3*SUM1/PREF
      WRITE(6,50) F(K), VARI
   50 FURMAT(1F10.3:1E20.5)
 2000 KHUS(K)=C2*C3*SUM1
      WRITE(6.1) PHI(KK)
    1 FORMATCHES 37H SPECTRAL DISTRIBUTION OF ROTOR SOUND ///
     130H WAKE TURBULENCE RELATED SOUND //17m RAUTALION ANGLE
                                                                  1-7-2//
     210X, IOH FREQUENCY TOX, BH SPL(DB)
                                           7)
      DO 10 I=1.NF
      VAR1=RHO5(I)/PREF
      IF(VAR1.LT.1.0) GO TO 10
      RHO5(I)=10.*ALOG10(VAR1)
   10 CONTINUE
      wRITE(6,2) (F(I),RHOS(I),I=1,NF)
    2 FORMAT(12X,1F10.2,1UX,1E2U.4)
 1000 CONTINUE
      RETURN
      END
```

```
SUBROUTINE ORIHI(SX, KPS, Uluz, UZO1, PHI, XLAM, B, KI, KS, DKDK)
      COMPUTES THE SUM OF THE COMPONENTS IN THE DIRECTION OF THE
      OBERVER FROM EACH BLADE OF THE ROTOR
C
      DIMENSION ZY(3,3), THE (30), YX(3,3), OX(3), OYY(3,3), K(3), V(3)
      INTRODUCE THE COMPONENTS OF THE FIRST ROTATION
C
      PI=3.14159
      ZY(1,1) = SIN(XLAM)
      ZY(1,2)=CUS(XLAM)
      ZY(1,3)=0.∪
      ZY(2,1) = -CUS(XLAh)
      2Y(2,2)=SIN(XLAM)
      ZY(2,3)=0.0
      4Y(3,1)=0.0
      ZY(3,2)=U.U
      ZY(3,3)=1.0
      THE NEXT ROTATION DEPENDS ON THE INITIAL BLAVE POSITION AS VOES
      THE OBSERVER RADIUS VECTOR
      NG=IFIX(B)
      DRDR=0.0
      00 10 K=1 +NB
      THE(K)=36U./d*FLUAT(K)
      THET=THE(N)*PI/180.
      D=N=R1*(1.-R5/R1*SIN(Phi)*CO5(TnET))
      R(1) = (R1*5IN(PHI) - R5*CUS(THET))/DEN
      R(2) = (-R5*5IN(THET))/DEN
      R(3)=(R1*COS(PHI))/DEN
       1X(1:1) =- 0 IN([HE])
       YX(1,2)=CUS(THET)
       YX(1,3)=0.00
       YX(2:1)=0.0
       YX(2,2)=U.U
       YX(2,3)=1.0
       YX(3,1)=CUS\{THET\}
       YX(3,2)=5IN(THET)
       YX(3,3)=0.0
       NOW SUM ON THE COMPONENTS TO GET FINAL VALUES IN OBSERVER FRAME
       DD=0.0
       DO 11 I=1,3
       V(I) = 0.0
       DO 11 J=1.3
       DO 11 L=1.3
    11 V(I)=R(L)*AY(I,J)*YA(J,L)+V(I)
       wRITE(6,30) (V(I),I=1,3)
    30 FORMAT(5H V(B) 3515.3)
       DETERMINE THE COMPONENTS IN THE DIRECTION OF THE OBSERVER
C
       DIPOLE TERMS
C
```

```
DO 12 I=1,2
      DO 12 J=1.2
      IF(I.EQ.1.AND.J.EQ.2) GU TO 13
      IF (J.EQ.1.AND.I.EQ.2) UO TO 131
      VAR1=SX(I)*SX(J)
      GO TO 12
   13 VAR1=-U1U2**2
      GU TO 12
  131 VAR1=-U2U1**2
   12 DO=DD+V(I)*VAR1*v(J)
   10 DRDR: 'RDR+DD
      wRITE(6,20) DRDR
   20 FORMAT(1E20.5)
C
      THIS COMPLETES COMPUTATION OF THE COMPONENTS IN THE
      DIRECTION OF THE OBSERVER
      RETURN
      END
      SUBRUUTINE TUNE(R1.B.FB. KHO.XLAM. K25.K5.U1.F)
Ç
      COMPUTES PURE TONES GENERATED BY STEADY BLADE FORCES AND
      THE MEAN VALUES OF THE STRESS TENSOR
      DIMENSION BES(200), CX(3), CYY(3, 3), JX(200), TYY(200), F(200),
     1RHU(2UU), HI(2U), TT(3U), DD(3U)
      DATA A0, P1, CG/342, 33.14129:1.4/
      PREF=20.E-06/A0**2
      PREF=PREF*PREF
      RATM=1.175
      C.O=MTAS
      NB=IFIX(B)
Ċ
      PROVIDE THE TENSOR AND FORCE COMPONENTS
      C1=1./(2.*PI*AO**2*R1)**2
      REV=RPS/(2.*PI)
      FAX=0.05*FB
      FT=0.95*FB
      DO 1 I=1,3
    1 5X(I)=0.0
      5X(1) = -FAX
      5X(2)=FT
      DO 2 I=1,3
      DO 2 J=1,3
    2 5YY(I,J)=0.0
      5YY(1:1)=1.0
      DO 1000 KK=1:1
      PHI(KK)=30.+10.*FLOAT(KK)
      PHI(KK) = 60 \cdot + 10 \cdot *FIOAI(KK)
      PHI(KK)=80.
      PHIP=PHI(KK)*PI/180.
      C2=(B/R5)**2
      C3=(B*RATM*U]*U1/(AO*RS*SIN(PHIP)))**2
```

```
C
                COMPUTE THE SPECTRUM
                CALL ORTHALSX, SYY, PHIP, XLAM, 10, KI, KS, DD, 11)
C
                COMPUTE 5 HARMONICS OF BLADE PASSAGE FREQUENCY
               NH=10
                DO 10 N=1 • NH
                F(N)=FLOAT(N)*REV*B
                ARG=2.*PI*+(N)*R5*S1N(PHIP)/AU
                NN = IFIX(B) * N + 1
                CALL NBESU(ARG, NN, BES)
                wRITE(6,30) ARG, BES(NN)
         30 FORMAT(16H BESSEL FUNCTION
                                                                                          2E20.51
                TYY(N)=0.0
                TX(N) = U_{\bullet}U
                DO 40 K=1.NB
                DO 40 L=1 + NB
                TX(N) = TX(N) + BES(NN) * BES(NN) * DD(N) * 
        40 TYY(N)=TYY(N)+BEO(NN)*BEO(NN)*TI(K)*TI(L)*2.**PI*F(N)
                THIS COMPLETES THE SPECTRAL LEVEL COMPUTATION - NOW CALL ROUTINE
           . TO PERFORM COORDINATE TRANSFORMATIONS
                VARI=C1*C2*TX(N)/PREF
                VARZ=C1*Co*TYY(N)/PKEF
                wRITE(6,20) F(N), VAR1, VAR2
        20 FORMAI(3(1F10.2,2F15.3))
                FNN=FLOAT(N)*FLCAT(N)
        10 RHU(N)=C1*C2*FNN*TX(N)
                WRITE(6,5)
           5 FORMATCIBLE 37H SPECTRAL DISTRIBUTION OF ROTOR SOUND
                                                                                                                                                              1/11
                DO 11 I=1 NH
                VARZ=RHO(1)/PREF
                IF(VAR2.LI.1.U) GO TO 11
                RHO(I)=10.*ALOG10(VAR2)
        11 CONTINUE
                WRITE(6,3)
                                               PHI(KK)
           3 FORMAT(/////36H SPECIRAL DISTRIBUTION OF TOME SOUND
             117H RADIATION ANGLE 1F5.2///
                                                   11X.8H SPL(DB)
             29H FREQ(H4)
                                                                                                        111
                wR11c(6,4)
                                               (F(I),RhU(I),I=I,NH)
           4 FORMAT(4(1F10.2,1F20.3))
   1000 CONTINUE
               RETURN
                END
                SUBROUTINE ORTH2(SX:SYY:PHI:XLAM; B:R1:RS:DRDR:TKTR)
C
               COMPUTES THE SUM OF THE COMPONENTS IN THE DIRECTION OF THE
C
               OBERVER FROM EACH BLADE OF THE ROTOR
               UIMENSION 4Y(3,3), THE(30), YX(3,3), 5X(3), SYY(3,3), K(3), V(3)
               DIMENSION DRDR(30), TRTR(30)
C
                INTRODUCE THE COMPONENTS OF THE FIRST ROTATION
```

```
PI=3.14159
      2Y(1,1)=51N(XLAM)
      ZY(1,2) = CUS(XLAM)
      ∠Y(1,3)=U.U
      ZY(2,1) = -COS(XLAH)
      ZY(2,2) = SIN(XLAM)
      ZY(2,3)=0.U
      ZY(3,1)=0.0
      2Y(3,2)=U.U
      2Y(3,3)=1.0
      THE NEXT ROTATION DEFENDS ON THE INITIAL BLADE PUSISTION AS DUES
C
C
      THE UBSERVER RADIUS VECTUR
      NB=IFIX(B)
      DO 10 K=1 + NB
      THE(K)=36U./B*FLUAT(K)
      THET=THE(N)*PI/180.
      DEM=R1*(1.-RS/R1*SIN(PHI)*CUS(IHE!))
      R(1)=(R1*5IN(PHI)-R5*CO5(THET))/DEN
      R(2) = (-RS*SIN(THET))/DEN
      R(3) = (R1*COS(PHI))/DEN
      YX(1,1) = -5IN(THET)
      YX(1,2)=CUS(THET)
      YX(1,3)=0.0
      YX(Z91)≐UeU
      YX(2,2)=0.0
      YX(2,3)=1.J
      YX(3,1)=CUS(THET)
      YX(3+2)=5IN(THEI)
      YX(3+3)=0+0
      NOS SUM ON THE COMPONENTS TO GET FINAL VALUES IN OBSERVER FRAME
      DD=0.0
      TT=0.0
      DU 11 I=1.3
      C \bullet O = (1)V
      DO 11 J=1,3
      DO 11 L=1.3
   11 V(I)=k(L)*YX(J,L)*ZY(I,J)+V(I)
      wRITE(6,20) (V(1), I=1,3)
   20 FORMAT(//31H OBSERVER VECTOR IN BLADE BASIS /3E2v.5//)
C
      DETERMINE THE COMPONENTS IN THE DIRECTION OF THE OBSERVER
C
      DIPOLE TERMS
      DO 12 I=1:2
   12 DD=DD+V(I)*SX(I)
      WRITE(6,30) DD
   30 FORMATILED FORCE COMPONENT
                                      1E20.5)
C
      QUADRAPOLES
      DO 18 I=1.2
      DO 18 J=1,2
   18 TT=TT+V(I)*SYY(I,J)*V(J)
      DRDR(K)=DD
   TO TRIR(K)=TT
      THIS COMPLETES COMPUTATION OF THE COMPONENTS IN THE
C
C
      DIRECTION OF THE OBSERVER
      RETURN
      END
```

#### 4.0 PROGRAM TONE

This model was set up in a computer program so that direct numerical computations of the time series described by the equation for the radiated sound could be made. This direct approach of calculating the actual time series is the difference between the present approach and those of other rotor models. Typically the analytical results for the rotor are Fourier transformed and reduced to a closed form (such as program ROTOR described herein). This approach normally requires that simplifications be made so that the closed form can be obtained. The advantage of the present approach is no simplifications in the analysis need be made.

The time series is computed for a sufficient number of values so that a good statistical sample will result. The time series is then Fourier transformed using a Fast Fourier Transform algorithm to yield the spectrum of the radiated sound. In other words, the model is used to generate a time series which is handled exactly as one would handle experimental data. Very complex source histories can be studied with no more effort than the very simple steady force case. For example, rotor wobble can be simulated in order to study how it affects the generation of sound; the individual blades can be allowed to vibrate as might occur in flutter cases; or each blade can be assigned a different value of force to determine the effect of such blade to blade differences as might be caused by manufacturing imperfections.

Of most importance, is that complex random effects can be included in this model, also. Such mechanisms as force fluctuations related to wake turbulence, inflow turbulence, or even rotating stalls can be studied. The

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way this must be done is to express the force fluctuation in a time series that has the required statistical nature. If the spectrum of the force fluctuation relative to the blade is known, then it is possible to generate a random time series which will give the same statistics as the known result. The methods for generating an auto-regres on analysis can be used to simulate the spectrum of the force on the blades. Once the time series are known, the results from the different blades may be combined in different ways to simulate different mechanisms of sound generation. For example, the effect of large scale turbulence can be simulated by allowing several of the blades to experience the same force fluctuation, or allow all of them to experience it. The case where there is no blade to blade correlation would model the wake related sound generation.

The idea of the model is to provide a tool where the various mechanisms which might produce appreciable sound generation can be evaluated. In addition, it is sought to set up the model in such a way that its usage will be reasonably simple and straightforward. As an example, if one wants to study the effect of different forces on each of the blades, he merely reads in the array of steady loads he wishes to rotor to have, and that is all. Rotor wobble is accounted for by replacing the velocity of the source, the rotor velocity, with a time dependent function describing the wobble characteristics.

## 4.1 Tone Noise Generation Model

The generation of pure tone sound due to the steady state forces on the rotor blading is studied in the model. In addition, an auto-regression method is used to write a time series which approximates a random force distribution resulting in broad band noise generation.

The model is based upon M.V. Lowson's development for rotating point forces. The development is done for a force per unit volume. In this representation only the point force case will be considered. Extension to the distributed case can be treated as an array of point forces where the array is distributed along the span as well as circumferentially. This has been done by the author and the mechanics are straightforward but the expense in computer time is correspondingly increased.

For a point force, the radiated sound in the far field can be written:

$$p(\vec{x},t) = \left[\frac{x_i \cdot y_i}{4\pi a_i r^2 (1-M_r)^2} \left\{ \frac{\partial F_i}{\partial t} + \frac{F_i}{1-M_r} \frac{\partial M_r}{\partial t} \right\} \right]_{t_R}$$

where the evaluation of the source terms of the retarded time

$$t_{R} = t - \frac{|\vec{x} - \vec{y}|}{a_{o}}$$

 $\mathbf{t}_{\mathrm{R}}$  = time of sound generation

t = time of observation, and  $|\vec{x} - \vec{y}|/a_0$  = propagation time.

The position vector  $\mathbf{r} = \mathbf{x} - \mathbf{y}$  can be written in the form

$$\sum_{i=1}^{3} (x_i - y_i) \stackrel{\triangleright}{e_i} \text{ in rectangular cartesian coordinates.}$$

The Mach number  $_{\rm r}^{\rm M}$  is the component of the source Mach number in the direction of the observer. It may be written

$$M_{r} = M_{s} \cdot r/|r|$$

or in components as

<sup>\* &</sup>quot;The Sound Field for Singularities in Motion," Proc. Roy. Soc., A, 236, 559, 1965.

$$M_{r} = \sum_{i=1}^{3} M_{i}(x_{i}-y_{i})/|r|$$

The components of the blade force F can be chosen to represent the thrust and torque loads on the individual blades. Using the blade stagger angle,  $\xi$ , write

$$F_1 = -F \cos \xi$$
  
 $F_2 = -F \sin \xi \sin \theta$   
 $F_3 = F \sin \xi \cos \theta$ .

Take the time derivatives of these force components:

$$\partial F_1/\partial t = 0$$
  
 $\partial F_2/\partial t = -F\Omega \sin \xi \cos \theta$   
 $\partial F_3/\partial t = -F\Omega \sin \xi \sin \theta$ .

The components of the position of the observer are written in polar form as

$$x_1 = r \cos \phi$$

$$x_2 = r \sin \phi$$

$$x_3 = 0 .$$

The location of the source is also written in polar form:

$$y_1 = 0$$

$$y_2 = R_s \cos \theta$$

$$y_3 = R_s \sin \theta.$$

Finally, the components of the source Mach number are

$$M_1 = 0$$

$$M_2 = -M \sin \theta$$

$$M_3 = M \cos \theta.$$

The value of the source Mach number is

$$M_s = R_s \Omega / a_o$$
.

The Mach number component  $M_{\mathbf{r}}$  may now be computed:

$$M_r = \sum_{i=1}^{3} M_i (x_i - y_i)/r$$
.

Substitution yields

$$\begin{aligned} \mathbf{M}_{\mathbf{r}} &= (\mathbf{r}_{1} \cos \phi)(0)/\mathbf{r} + (\mathbf{r}_{1} \sin \phi - \mathbf{R}_{s} \cos \theta)(-\mathbf{M}_{s} \sin \theta)/\mathbf{r} \\ &= -(\mathbf{r}_{1}/\mathbf{r}) \mathbf{M}_{s} \sin \phi \sin \theta + (\mathbf{R}_{s}/\mathbf{r}) \mathbf{M}_{s} \cos \theta \sin \theta, \end{aligned}$$

so that to the first order

$$M_r = -M_s(r_1/r) \sin \phi \sin \theta$$
.

The time derivative of the Mach number becomes

$$\partial M_r/\partial t = -M_s(r_i/r) \Omega \sin \phi \cos \theta$$
.

All the terms required for the computation of the pressure radiated are now complete. The radiated sound is

$$\begin{split} p(\vec{x},t) &= [\frac{F}{4\pi a_0 r^2 (1-M_r)^2} \{ \frac{r_1 \sin \phi - R_s \cos \theta}{r} \; (-\Omega \sin \xi \cos \theta) \\ &\quad - \frac{R_s \sin \theta}{r} \; (-\Omega \sin \xi \sin \theta) + \frac{1}{1-M_r} \frac{\partial M_r}{\partial t} \; [\frac{r_1 \cos \phi}{r} \; (-\cos \xi) \\ &\quad + \frac{r_1 \sin \phi - R_s \cos \theta}{r} \; (-\sin \xi \sin \theta) + \frac{-R_s \sin \theta}{r} \sin \xi \cos \theta] \} ]. \end{split}$$

And, expanding:

$$p(\hat{\mathbf{x}},t) = \left[\frac{F}{4\pi a_0 r (1-M_r)^2} - \frac{-r_1 \Omega \sin \phi \sin \xi \cos \theta}{r} + \frac{R_s \Omega \sin \xi}{r} (\cos^2 \theta + \sin^2 \theta) + \frac{1}{1-M_r} \frac{\partial M_r}{\partial t} \left[\frac{-r_1 \cos \phi \cos \xi}{r} - \frac{-r_1 \sin \xi \sin \phi \sin \theta}{r}\right]\right].$$

The solution reduces to the form

$$\begin{split} p(\overline{x},t) &= \frac{F}{4\pi a_0 r^2 (1-M_r)^2} \left[\Omega \sin \xi \left(R_s - r_1 \sin \phi \cos \theta\right) \right. \\ &\left. - \frac{1}{1-M_r} \frac{\partial M_r}{\partial t} \left(r_1 \cos \phi \cos \xi + r_1 \sin \xi \sin \phi \sin \theta\right)\right]. \end{split}$$

This will give the radiated sound from each of the blades. The above expression is to be evaluated at the retarded time. This will require some further manipulations.

$$t_R = t r/a$$
 where  $r = |\hat{x} - \hat{y}|$ 

square the distance r

$$r^{2} = (x_{i}^{-}y_{i}^{-})^{2} = (r_{i}^{-}\cos\phi)^{2} + (r_{i}^{-}\sin\phi - R_{i}^{-}\cos\theta)^{2} + (R_{i}^{-}\sin\theta)^{2}$$

$$= r_{i}^{2} - 2 r_{i}^{-}R_{i}^{-}\sin\phi\cos\theta + R_{i}^{2}.$$

Now,  $r_1 >> R_s$ , so it will be sufficient for the far field solution to write

$$r^2 = r_1^2 - 2 r_1 R_s \sin \phi \cos \theta$$

or, equivalently,

$$r^2 = (r_1 - R_s \sin \phi \cos \theta)^2 - R_s^2 \sin^2 \phi \cos^2 \theta .$$

For the far field solution we can therefore use

$$r = r_1 - R_s \sin \phi \cos \theta$$
.

The retarded time can be written as

$$t_{R} = t - r_{1}/a_{0} + R_{s}/a_{0} \sin \phi \cos [\theta]$$
,

where the  $[\theta]$  is the retarded value of the blade location.

This source position may be written as

$$[\theta] = \Omega t_R + \theta_{t_R=0} = \Omega(t - r_1/a_0) + \frac{\Omega R_s}{a_0} \sin \phi \cos [\theta] + \theta_{t_R=0}.$$

Now in the solution for the radiated sound substitute  $t_R$  for t and  $[\theta]$  for  $\theta$ , the radiated sound pressure \*-comes

$$\begin{split} p_K(\hat{x},t) &= \frac{F}{4\pi a_0 r^2 (1-[M_r])^2} \left\{\Omega \sin \xi (R_s - r_1 \sin \phi \cos [\theta]_k) \right. \\ &\left. - \frac{r_1}{(1-[M_r]_k)} \left[\frac{\partial M_r}{\partial t}\right]_k \left(\cos \xi \cos \phi + \sin \xi \sin \phi \sin [\theta]_k)\right\} \end{split}$$

where: 
$$r = r_1 - R_s \sin \phi \cos [\theta]_k$$

$$[M_r]_k = -M_s \sin \phi \sin [\theta]_k$$

$$[\partial M_r/\partial t]_k = -M_s \Omega \sin \phi \cos [\theta]_k$$
,
with:  $[\theta]_k = \Omega(t - r_1/a_0) = (\Omega R_s/a_0) \sin \phi \cos [\theta]_k + \theta_k, t_R=0$ 

$$\theta_{k,t=0} = \text{location of kth source at } t_R = 0$$
.

The total sound from all the rotor blades becomes

$$p(\vec{x},t) = \sum_{K=1}^{B} p_{k}(\vec{x},t) .$$

## 4.2 How to Use Program TONE

As was seen in the previous section, the model used to predict the sound radiation generates a discrete time history using the solution for a rotating array of forces, then treats that history in the same way one would treat experimental data.

We previously mentioned the flexibility of this approach. This flexibility is achieved in the program by changing the program listing. A multiple option approach could have been taken but this is wasteful of computer time and assumes one knows all the options which will be needed. The reason for this approach was to provide a flexible tool; however, it does depend upon the operator's ability to change the Fortran statements used to generate the time series. This is easily done since the equations are short and the program is straightforward. The part of the program actually used to generate the time series is about 20 cards long.

The form of the program set up here is for the case where the force on each of the blades is the following function of time

$$F(t) = F_{B} (1 + C_{d}x(t))$$

where  $F_B$  is the steady state blade force,  $C_d$  is a dynamic loading coefficient, and x(t) is a time series simulating the unsteady force fluctuations on the blade. Depending upon the particular mechanism, x(t) can be chosen to simulate either wake related force fluctuations or the fluctuations caused by inflow turbulence interacting with the airfoil. Processes of this type can be represented using autoregressive processes. This will be discussed in section 4.5 below.

# 4.3 Program Inputs

Input to the program is done using cards. Four cards are required to run the program in its present form.

# CARD 1, FORMAT(115)

NOPT = 0, no plots

= 1, plot the time history

= 2, plot the sound spectrum

= 3, plot both the history and the spectrum

NOPT controls the type of output desired. Two CALCOMP subroutines are contained in the program so that the time history for the process can be examined and/or the spectrum of the radiated sound can be plotted. If neither plot is desired then listings of the time history and the spectrum will be the only output.

# CARD 2, FORMAT (7F10.2)

BE	bandwidth desired in the spectrum	(Hz)	
FMAX	maximum frequency in the spectrum	(Hz)	
See Section 4.4 f	or the implications of these selections.		
CARD 3, FORMAT(7F10.2)			
ZR	number of rotor blades	()	
ХI	blade stagger angle, ueasred from blade chord to radial plane passing through rotor axis	(DEG)	
PHI	radiation angle, measured from inlet rotor axis	(DEG)	
RPM	rotor speed	(RPM)	
RS	radial distance to source	(M)	
R1	radial distance to observer	(M)	
F	magnitude of force om each blade	(KG)	
CARD 4, FORMAT (7F10.2)			

CDYN	dynamic force coefficient	()
Al	autoregression coefficient	()
۸2	autorograpsion anafficient	()

See Section 4.5 for a discussion of the selection of the autoregression coefficients.

# 4.4 Time Sampling

The setting of FMAX and BE determines the sampling rate and the total number of required samples. Letting

$$f_{max} = FMAX$$

$$B_e = BE$$

we can illustrate how this is one. First, estimate the number of samples required as

$$N = 2 f_{max}/B_e$$
.

Since we will use a Fast Fourier Transform to find the spectrum, the number of samples must be of the form  $N^{\dagger}=2^{m}$  where m is an integer. We choose m such that

$$2^{m-1} < N \leq 2^m.$$

Then compute  $N^{T} = 2^{m}$  samples of the time series. The new bandwidth becomes

$$B_e^{\dagger} = 2 f_{max}/N^{\dagger}$$
.

The sampling rate for the time series is

$$H = 1/(2f_{max}) .$$

# 4.5 Use of Autoregression Processes

A second order autoregression process is used in the current form of the program to represent the force fluctuations. This process may be written

$$x(t) = a_1 x(t-1) + a_2 x(t-2) + Z(t)$$

where  $a_1$  and  $a_2$  are the autoregression coefficients (A1 and A2 in the program. Z(t) is a random number selected using a random number generator.

A time series is generated separately for each blade. If there is to be no correlation between different blades (as for wake related forces) then Z will be taken from a different random series for each blade. If correlation is desired between blades then the time series can be selected to reflect the correlation. Correlation would be expected to exist between blades for the mechanism of inflow turbulence.

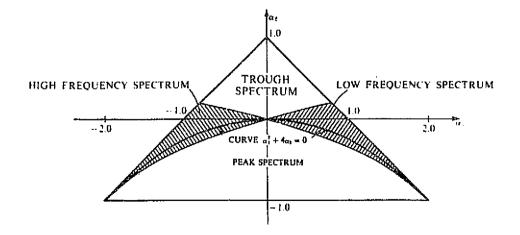
The main idea is to fit the time series to represent what is desired, then let the program compute the resulting sound radiation.

The spectrum for the second order process above can be solved for directly. The spectrum is

$$G_{xx}(f) = H\sigma_z^2/(1 + a_1^2 + a_2^2 - 2a_1(1-a_2) \cos 3\pi fH - 2a_2 \cos 4\pi fH)$$
  
- 1/2H < f < 1/2H.

Selection of  $a_1$  and  $a_2$  gives the spectral shape to be expected from x(t).

A plot of  $a_1$  and  $a_2$  for different spectral shapes is shown below to give an idea of the values of the coefficients needed for particular shapes.



A peaked spectrum is what we would expect for a wake related sound generation mechanism. A low frequency spectrum would be expected for the cases of inflow turbulence. The frequency where the peak will occur is givey by

$$\cos 2\pi f_0 H = -a_1 (1 - a_2)/4a_2$$
.

As may be expected, some experimentation will be required to fit the process to an actual experimental spectrum.

To obtain more complicated power spectral shapes higher order processes may be needed. These can be handled as easily as the above on the computer, but the preliminary efforts to get a particular spectrum increase.

For a good general discussion of the above method the reader is referred to SPECTRAL ANALYSIS AND ITS APPLICATIONS by G.M. Jenkins and D.G. Watts (1969).

If more simply definable fluctuations are needed these can be used for x(t). For example, inlet distortion or the effect of another blade row can be simulated by a Fourier series representation of the force fluctuation resulting from the distortion. A simple cosine with period equal to the stator spacing will give a good qualitative model of blade row interaction noise.

The model can also be extended to account for span distributions of the blade force. This is straightforward but the computer time required does increase substantially.

```
42
4.6 Program Listing
      PROGRAM TONE (INPUT + OUTPUT + TAPES = INPUT + TAPE6 = OUTPUT)
      COMPUTE SOUND RADIATION FROM A ROTATING ARRAY
C
      OF POINT FORCES
      COMPLEX C
      DIMENSION PRAD(1100) , THEP(20) , THE(20) , THER(20) , THERP(20)
      DIMENSION C(1024), B(2,1024), 1nV(206), M(3), S(256), AMP(1024),
     15PL(1024) , FREG(512) , PRA(1024) , L(1024) , X(4, 1024) , DATO(2048)
      EQUIVALENCE (C.B)
      NUAR = MARMONICS TO DE ANALYZED
C
      NOPI = OPIION
      BE = FREQUENCY BANDWIDTH DESIRED
C
C
      ZR = NUMBER OF RUTOR BLADES
      XI = STAGGER ANGLE, MEASURED FROM FAN AXIS (DEG)
C
C
      PHI = RADIATION ANGLE - MEASURED FROM FAN AXIS
C
      RPm = ROTUR SPEED (RPM)
C
      RS = SOURCE RADIUS (M)
C
      RI = OBSERVER RADIUS (M)
      F = FORCE ON LACH ROTOR BEAUE (KU)
Ç
      CDYN = DYNAMIC LOADING - PER CENT OF TOTAL FORCE
C
C
      A1 = AUTO-REGRESSION CONSTANT
      A2 = AUTO-REGRESSION CONSTANT
C
            X(J_{\bullet}I) = A1*X(J_{\bullet}I-I) + A2*X(J_{\bullet}I-2) + Z(I)^{*}
\mathsf{C}
      Z(I) = RANDOM VARIABLE
      DATA PIDAU/3e1415903420/
       INPUT MI SUCH THAT C HAS LENGTH N=2**MI
\mathsf{C}
      READ(5,1) NHAR, NOP
     1 FORMAT(2I)
      READ(5,2) BE
       OPTION = 0 NO PLOTS
C
C
       OPTION = 1 PLOT TIME HISTORY
Ċ
       OPTION = 2 PLOT SPECTRUM
       OPTION = 3 PLOT BOTH TIME HISTORY AND SPECTRUM
       READ(5,2) ZR,XI,PHI,RPH,RC,RL,F
       READ(5,2) CDYN,A1,A2
     2 FURMAT(7F10.2)
C
       CONVITION INPUT DATA
       CMFT = 3.28
       RS = RS*CMFT
       K1=R1*CMF[
       F≃F*2.21
```

FMAX=FLOAT (NHAR)\*RPM/60.\*ZK

FMAX=10000

DO 75 I=1:10

N1=IFIX(2.\*FMAX/BF)

REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR

```
N2=2**I
      IF(N2.GT.N1) GC TO 71
   75 CONTINUE
   71 NOAMP=NZ
      \sqrt{1} = I
C
       THE MAXIMUM NUMBER OF POINTS ARE 2**10 (1024)
      BE=2.*FMAA/FLOAT(NSAMP)
      XUMEG=RPM*2.*PI/60.
      XIP=XI*PI/18J.
      PHIP=PHI*PI/150.
      JINPHI=SIN(PHIP)
      CUSPmI=CUS(PHIP)
      SINXI=SIN(XIP)
      CUSXI=COS[XIP]
      XJJO=RS#XOmEG/AO
      NZR=ZR
      RANDOM FUNCE ON THE ROTOR DEADED MODELED BY UNCORRELATED
C
      SECUND DRUER PROCESS
      IX=2**24+3
      NRAND=NSAMP
      DU 31 J=1, NZR
      U1+X1=X1
      CALL RAND(IU, IX, 1, NRAND, 4)
      V \circ I = (L \circ V) X
      X(J, Z) = I_{a,U}
      DO 31 I=3 MSAMP
   31 X(J_*I) = A1*X(J_*I-I) + A2*X(J_*I-2) + \angle(I)
C
      WRITE INPUT DATA
      wKITE(G=20) ZR+XT+KPM+F+RS+PHI+RI
   20 FORMATCHESSIR RADIATION OF GOODD FROM A ROTATING ARRAY OF FORCES
     1///2011 NUMBER OF ROTUR BLADES - 110.0/2011 BLADE STAUGER ANDLE
     21F5.2/18H ROTOR SPEED (RPM)
                                     1010-2/120 blade FORCE IF10-2/
     331H RADIAL LUCATION OF POINT FUNCE
                                              160.2/
     416H RADIATION ANOTE: 155.2/160 OBSERVER RADIUS (155.1///)
      wRITE(6,24)
                    FMAX .BE
   22 FORMAT(//18H MAXIMUM FREQUENCY
     11r20-3,150 BANDWIDTH (MZ)
                                   15 10 a 4 / / )
      nRITE(6,2) CDYN,AI,12
   23 FURMATIZAM RANDUM FUNCE FEDETUATIONS
     137H X(T) = A1*X(I-1) + A2*X(I-2) + Z(I)
     223H DYNAMIC COEFFICIENT = IFIU.D /
     30H AI = \botF10.3.10X.0H AZ = \botF10.0
C
      INITIALIZE BLADE POSITIONS
      UU IO I=1 NZR
      1=1v
   10 THE(I)=2.*PI/ZR*(UI-1.)
      COMPUTE TIME SERVES DASED ON RETAINING SUFFICIENT
C
C
      INFORMATION FOR 10 HARMONICS .....
```

```
C
      50, SAMPLE AT 20 SAMPLES PER DEADE SPACING
C
      OCT TIME INCREMENT
      Fن=F
      DI=0.5/FMAX
      D. 200 K=1*NSAMP
      JK=K
      T=DI*(UK-i.)
      COMPOSE SOUND RADIALION FROM THE SEADE ARRAY
      PRAD(K)=0.0
      DU 300 J=1.NZR
      U=U
      IF(K.NE.1) GO TO 201
      IHEP(J) = IHE(J)
      JU TU 302
  301 THEP(J)=InERP(J)
  302 CONTINUE
      THERP(J) = IHER(J)
      X.R=-XNo*oINPHI*oIN(FalR(J))
      ロXHR=-X (つきXOMEG*っIMPhI*Cの5(lncR(j)))
      R=R1-R0*01MPH1*C05((HER(J))
      F=FJ*(1.+CDYN*X(J,K))
      VARI=F/((4.#PI#AUxRX*2)*(1.-XAR)#*2)
      VAK2=XCAEO#51NPH1#(K5-K1*51NPH1*CO5(THEK(J)))
      VAR3=-R1*DER/(1 - - XMR)*(CC3A1*CO3P::11+
     1-1/X1 #5[hfhl #5[n(THEn(U)))
      POLADE=VARI*(VAR2+VAR3)
  300 PRAD(K) =PRAD(K) +PREADE
  200 CUNTINUE
      Into COMPLETES COMPOTATION OF THE TIME SERVES FOR
      ONE RADIATION ANGLE
      (AMPCINET=16(1)(MAdel) (Teed)
   21 FURNAT(4(0X,115,5X,1E15,3))
     USAMP=NSAMP
C
     FIND THE MEAN VALUE
     ひらいまかしたり
      DO 400 I=1:NSAMP
  400 PSUM=PSUM+PRAC(I)
      PHEAN=PSUM/USAMP
      WRITE(6.30) PMEAN
   30 FURMAT(///29M MEAN KADIA/ED JOUND PREJSURE 1620.5///)
      DU 500 I = I . NSAMP
  500 PRA(I)=PRAD(I)/PMFAN
      IF(NOPT.EQ.1) GO TO 701
      IF(NOPT.EJ.4) GO TO 701
```

GO TO 702

701 CUNTINUE

```
C
       CONDITION THE DATA FOR THE TIME PLOT
C
       FIND MAXIMUM AND MINIMUM VALUES IN THE PRESSURE ARRAY
       PMAX=-999 & PMIN=999
       DU 600 I=1:NSAMP
       if(PRA(1)*LT*PMIN) PMIN=PRA(1)
       IF (PRA(I) .GT.PMAX)
                            PMAX=PRA(I)
  600 CONTINUE
       PLOT THE NORMALIZED ACOUSTIC PRESSURES
C
       CALL TPLOT (PRADNOAMP DOTOPHINOPHINA PNAK)
  702 CONTINUE
C
      PROVIDE ARRAY C
      DO 40 I=1 NSAMP
       I I = 2 * I
   40 DATO(II-1)=PRAD(I)
      NNN=Z*NSAMP
      ARITE(6,41)
                    (Nispie I = I • (I ) O (AU)
      CALL FOUR = (DATO = NSAMP = -1)
      DU 70 I=1 * NSAmP
       1 * _ = I I
   70 C(I)=CMPLX(DATO(I]-1) *DATO(II))
      ARRAY C NOW CONTAINS THE PREQUENCY COMPONENTS
      COMPUTE AMPLITUDE AND PHASE ANOLE FORM
      ARITE(6,41) (C(1),1=1,50)
   41 FURMAT(2(=UX, 1E10, 3, 5x, 1c15.0))
      NF=NSAMP/2
      DU 50 I=1=NF
      AmP(I) = CAus(C(I))
      AMP(I) = AMP(I)/NE
   50 SPL(I)=20.*ALUGIU(AMP(I)/20.*E-06)
C
      USE FAST FOURTER TRANSFORM TO EXPRESS IN TERMS OF FREGUENCY
\mathbf{C}
      COMPUTE THE FREGUENCY ARKAY
      F. AX=1./(2.*DT)
      DF=FMAX*2./FLOAT(NSAMP)
      DO 60 I=1+NF
      ∪1=1
   60 FREG(I)=BE*UI
      4KITE(6,61)
   01 FORMATI//Z4H RADIATED SOUND SPECTROM
                                                 111
      MRIIE(6,64) (FREC(I), SPL(I), I=1, NF)
   62 FORMAT(4(1F10.2,5X,1F10.2,5X))
```

```
IF(NOPT.EQ.2)
                     GO TO 703
      IF (NUPT . Ew. 4) GU TU 703
      50 TO 1060
  703 CONTINUE
      NOW PLOT THE SPECTRON OF THE RADIATED SOUND
      CONVITION THE DATA FOR THE SPECIFAL PLOT
      NF=NSAMP/4
      CALL FPEO! (SPE#FREG*NF)
 1000 CONTINUE
      3 Jup
      END
      JUBRUULINE FUURI(DATA = N = I SIGN)
C
      A SIMPLE FAST FOURIER TRANSFURM
      DIMENSION DATA(2048)
      PI=ACUS(-10)
      TP[=2.*P]
      120=2
      IP3=IP0*N
      I3REV=1
      DO 50 I3=1•IP3•IP0
      IF(13-13REV)15,20,20
   10 TEMPREDATA(13)
      TEMPI=DATA(I3+1)
      DATA(I3)=DATA(I3KEV)
      DATA(15+1) = DATA(13REV+1)
      DATA(I3REV) #TEMPR
      DATA(I3REV+1)=TEFPI
   20 IP1=IP3/2
   30 IF(13REV-IP1) 50,50,40
   40 I3RLV=13KLV-IP1
      IP1=1P1/2
      IF(IP1-IPU)50ヵ30ヵつむ
   50 I3REV=I3REV+IP1
      IP1=IP0
   60 IF(IP1-IP3) /0,100,100
   70 1P2=1P1*2
      THEIA=[PI/FLOAI(ISIGN*IPZ/IPU)
      UINTH=STALTHETA/2.)
      no[|K=-2.*0]N|H*0[N]n
      NOTPI=SIN(THEIA)
      WR=1.
      wi=Ca
      DO 90 Il=1:IP1:IP0
      DO 80 I3=11, IP3, IP2
      12A=13
      12B=12A+1P1
      IEMPR=WR*DATA(IZD)-wI*DA(A(IZC+1)
      ICOP1=4R*UATA(120+1)+41*UATA(120)
      DATA(12B)=DATA(12A)-TEMPR
      UATA(126++)=DATA(12A+1)-IEMPI
      DATA(12A) = DATA(12A) + TEMPR
   80 DATA(12A++)=DATA(12A+1)+1E/4P1
```

```
WK=WK*WSTPK-WI*WSTPI+WK
   90 wl=wl*WSTPR+TEMPR*WSTP1+wl
      IP1=IP2
      GO TO 60
  100 RETURN
      END
      SUBROUTINE TPLOTIPRAD, NOAMP + D1 + PMIN + PMAX + NPAS)
      DIMENSION PRAD(1100) +T(1100)
C
      INITIALIZE THE PLOT
      CALL PRNTUN
      PLUT SIZE TO BE 5 BY 7 INCHES
C
      SET OBJECT SPACE
      NPAS IS THE NOMBER OF BEASE PASSAGES TO BE PECTICA
      UPAS = NPAS
      IMAX=UPA5*20**DI
      CALL STS2UB(2.,9.,2.,7.)
      CALL SISUBJIO. . INAX . PMIN . PMAA)
      COMPTRUCT AVER
C
      CALL JINDIV(1.2)
      CALL AXLILI
      CALL JAXLII
      CALL SAXLIR
C
      LABEL SCALES
      (2 t ) VICNIC JAA
      CALL STNUEC(U)
      CALL NOSLIB
      CALL NOSLIL
      TITLE SCALES
C
      CALL SINCHR(11)
      CALE TITEED(11H TIME (SEC) )
      CALL STNCHR(29)
      CALL TITLEL(29H FAR FIELD ACOUSTIC PRESSURE )
C
      GENERATE THE TIME ARRAY
      NT=NPA5*20
      11=0.0
      DO IO I=I NT
      1 = I U
   10 I(I) = II + DI * (UI - I - I)
      PLUT THE DATA USING STRAIGHT LINES
C
```

TEMPR=WR

```
CALL STAPIS(NI)
      CALL SLEILI(T, PRAD)
С.
      TERMINATE PLOTTING
      CALL EXITPL
      RETURN
      FNO
      SUBRUUTING FPLOT(SPL »FREG»NF)
      DIMENSION SPL(1024) »FREW(1024)
C
      INITIALIZE THE PLOT
      CALL STCCON(48H 10NE NOISE GENERALION SPECTROM
C
      PLUT SIZE TO BE 5 BY T INCHES
C
      SET UDJECT SPACE
      CALL 3/3200(2.99.52.97.)
      CALL STOUGU(10.,10000.,50.,100.)
C
      CUNSTRUCT AXES
      CALL SINDIV(30,20)
      CALL AXLGLI
      CALL JAXLUI
      CALL JAXLIK
C
      LASEL SCALES
      CALL STADIV(3,10)
      CALL STADEC(U)
      CALL NOSEIL
      CALL NOLGO
C
      ITILE SCALES
      CALL SINCHR(15)
      CALL TITLEB(15H FREQUENCY (HZ) )
      CALL SINCHR(37)
      CALL IIILEL(3/H REDIATED SPL (DD RE 20 MICRO M/ M*#2) )
C
      PLUT THE DATA USING STRATUM LINES
      CALL STAPISIAF)
      CALL SLIGHT (FREG. SPL)
     TERMINATE PLOTTING
C
      CALL EXITPL
      RETURN
```

END

#### 5.0 PROGRAM SDATA

Program SDATA is used to perform correlation and spectral analysis on discrete time series. The particular operations carried out on two given time series are:

- Autocovariance function for each sample and cross covariance between the two samples
- 2) Autocorrelation function for each sample and cross correlation between the two samples
- 3) Autospectrum for each sample
- 4) Magnitude and phase representation of cross spectrum between the two samples
- 5) Squared coherency function

The analysis used as the basis for the program is that presented in SPECTRAL ANALYSIS AND ITS APPLICATIONS, by G.M. Jenkins and D.G. Watts. The method used is exactly that recommended in this reference.

Two input possibilities exist. The first is to input two time series of arbitrary length. For this case the program will compute all the above covariances, correlations, and spectral quantities. The second possibility is to input two covariance functions. In this case the program will only carry out the spectral analysis. Some electronic instruments have become available recently which quickly compute correlation functions. This program can be used in conjunction with these instruments to obtain the spectral representation of the data.

A classical Fourier transform was used in the program. For this reason long samples, in terms of correlation lags, will require substantial computer time. Therefore, a Fast Fourier Transform program should be used for large samples.

# 5.1 Outline of Computations

This outline is substantially the same as that presented by Jenkins and Watts (pages 382 and 383).

Two time series of data,  $x_{t1}$  and  $x_{t2}$ , sampled at increments of H sec for a total of N points. For convenience H is assumed equal to one. The frequency range is then  $0 \le f \le 1/2$  Hz. For non-unity values of H the frequency range is  $0 \le f \le 1/2$ H. The actual spectral levels are also to be multiplied by H to obtain quantitatively correct values.

The computations are:

- (1) For the x<sub>t1</sub> data:
  - (a) the autocovariance estimate is

$$c_{11}(k) = \frac{1}{N} \sum_{t=1}^{N-k} (x_{1t} - \overline{x}_1) (x_{1t+k} - \overline{x}_1) \quad 0 \le k \le M-1$$

where M is the number of time lags in the estimate and the mean value is

$$\overline{x}_1 = \frac{1}{N} \sum_{t=1}^{N} x_{1t}$$

(b) the smoothed spectral estimate using a Tukey window

$$\overline{c_{11}}(j) = 2 \{c_{11}(0) + 2 \sum_{k=1}^{N-1} c_{11}(k) \text{ w (k) } \cos \frac{\pi k j}{F} \} \quad 0 \le j \le F$$

F is a measure of the spacing of the frequency points. The smoothed spectral estimates are to be computed at  $0,1/2F,\ldots,1/2$  where F is of the order 2 to 3 times M. The Tukey window w(k) is defined by

$$w(k) = \frac{1}{2} (1 + \cos \frac{\pi k}{M})$$
  $|k| \le M$ 

- (2) For the x<sub>t2</sub> data:
  - (a) the autocovariance function estimate

$$c_{22}(k) = \frac{1}{N} \sum_{t=1}^{N-k} (x_{2t} - \overline{x}_2) (x_{2t+k} - \overline{x}_2)$$
  $0 \le k \le M-1$ 

with the mean value

$$\overline{x}_2 = \frac{1}{N} \sum_{t=1}^{N} x_{2t}$$
.

(b) the smoothed spectral estimate

$$\overline{c}_{22}(j) = 2\{c_{22}(0) + 2\sum_{k=1}^{M-1} c_{22}(k) \le (k) \cos \frac{\pi k j}{F}\}$$
  $0 \le j \le F$ 

where the same window is used (Tukey) for w(k).

- (3) For the  $x_{t1}$  and the  $x_{t2}$  data:
  - (a) the cross covariance estimate

$$c_{12}(k) = \frac{1}{N} \sum_{t=1}^{N-k} (x_{1t} - \overline{x}_1) (x_{2t+k} - \overline{x}_2) \qquad 0 \le k \le M-1$$

$$c_{21}(k) = c_{12}(-k) = \frac{1}{N} \sum_{t=1}^{N-k} (x_{1t+k} - \overline{x}_1) (x_{2t} - \overline{x}_2) \qquad 0 \le k \le M-1$$

(b) the even and odd cross covariance estimates

$$\ell_{12}(k) = \frac{1}{2} \{c_{12}(k) + c_{12}(-k)\} \qquad 0 \le k \le M-1$$

$$q_{12}(k) = \frac{1}{2} \{c_{12}(k) - c_{12}(-k)\} \qquad 0 \le k \le M-1$$

(c) the smoothed co- and quadrature spectral estimates

$$\overline{L}_{12}(j) = 2 \{ \ell_{12}(0) + 2 \sum_{k=1}^{M-1} \ell_{12}(k) \le (k) \cos \frac{\pi j k}{F} \} \qquad 0 \le j \le F$$

$$\overline{Q}_{12}(j) = 4 \sum_{k=1}^{M-1} q_{12}(k) w (k) \sin \frac{\pi j k}{F}$$

$$1 \le j \le F-1$$

note that  $q_{12}(0) = 0$  and that  $Q_{12}(0) = Q_{12}(F) = 0$ .

(d) the smoothed cross amplitude spectral estimate

$$A_{12}(j) = \sqrt{L_{12}^2(j) + Q_{12}^2(j)}$$
  $0 \le j \le F$ 

(e) the smoothed phase spectral estimate

$$\overline{F}_{12}(j) = \arctan \left\{-\frac{\overline{Q}_{12}(j)}{\overline{L}_{12}(j)}\right\} \qquad 0 \le j \le F$$

(f) the smoothed squared coherency spectral estimate

$$\overline{K}_{12}^{2}(j) = \frac{\overline{A}_{12}^{2}(j)}{\overline{c}_{11}(j) \ \overline{c}_{22}(j)} \qquad 0 \le j \le F$$

#### 5.2 Correction for Bias Error Reduction

When there is a large delay in the correlation a large error can result in the coherency and phase spectrum. This bias error can be reduced by shifting the cross covariance function so that the maximum correlation occurs at zero time lap.

The way this correction is made in the present program is to search for the time lag corresponding to the largest a lute value of covariance. A new covariance function is then generated such to the peak occurs at the

zero time lag. This function is Fourier transformed and the phase shift introduced by the time shift is applied to the spectral estimate to correct it back. A consequence of the generation of a new covariance function is that it necessarily will contain fewer terms than the original. This results in a wider frequency bandwidth in the spectral estimate. This is why the program will seem to generate different bandwidths for different batches of data even when the same number of lags are called out in the input.

## 5.3 Input to Program

Two possibilities exist for input to this program. The first is to read in two time series of variables for which correlation and spectral computations are required. This is obtained from data card one by setting the variable OPTION = 1, FORMAT(115). If OPTION is not set equal to one the program will read in the data as if it were covariance functions. Input for OPTION = 1 is described in Section 5.3.1 and for OPTION # 1 in Section 5.3.2.

CARD 1, FORMAT(1T5)

OPTION = 1 read in time series

# 1 read in covariance functions

#### $5.3.1 \quad \text{OPTION} = 1$

CARD 2, FORMAT (215)

NSAMP number of points in the time sample

MLAG number of time lags desired in the covariance functions typically MLAG is chosen to be approximately one tenth as large as NSAMP.

CARD 3, FORMAT(1F10.2)

DELT time increment in samples

(Sec)

The remaining inputs under this option are the actual values of the variable in the time series. They are read 7 values to each card in the FORMAT(7F10.2). The number of cards required depends upon the size of the sample. The computer call is

DO 10 I = 
$$1,2$$

10 READ(5,2) 
$$(X(J,I),I = 1,NSAMP)$$

This is the total input required for this option.

## 5.3.2 OPTION $\neq 1$

CARD 2, FORMAT (2F10.2)

XLAG number of values in the covariance function samples

DELT time increment in the functions (Sec)

The remaining cards are used to read in the covariance functions. In the present format the functions are read in as follows.

DO 10 
$$I = 1,2$$

$$DO 10 J = 1,2$$

10 READ(5,2) (COV(K,I,J), 
$$Y = 1,M1$$
)

where M1 = XLAC + 1 and the indices I,J mean the following:

 $COV(K,1,1) = C_{11}(k) = autocovariance function for series 1, k = 0, %$ 

 $COV(K,2,2) = C_{22}(k) = autocovariance function for series 2, k = 0,M$ 

 $COV(K,1,2) = C_{12}(k) = cross covariance function for positive time lags, <math>k = 0,M$ 

 $COV(K,2,1) = C_{21}(k) = cross covariance function for negative time lags, <math>k = 0,M$ 

The format used to read in these functions is FORMAT(7F10.2). This completes the input requirements for this option.

# 5.4 Program Input

The output of the present form of this program is simply a listing of each of the functions computed. The list of functions computed was presented in Section 1.0.

## 5.5 Program Listing

```
PROGRAM SDATA (IMPUT + OUTPOT + LAPES = INPOT + IMPE6 = OUTPOT)
      A STATISTICAL DATA ANALYSIS PRODRAM WHICH COMPULES THE FUNCTIONS
Ċ
C
      AUTO COVARIANCE AND CROSS COVARIANCE AS WELL AS
C
      AUTO AND CROSS SPECTRUM
      DIMENSION X(1024-2), COV(101,2,2), 2(200)
\mathbf{C}
      READ IN THE TIME SERIES
C
      NSAMP = NUMBER OF TIME SAMPLES
C
      MLAG = NUMBER OF CORRELATION LAGS
C
      DELT = TIME INCREMENT (SEC)
C
      X(I)J) = THE TWO SAMPLES TO BE ANALYZED
      DATA PI/3.14159/
      READ(5.1) OPTION
                    READ TIME SERIES OTHERWISE READ COVARIANCES
C
      OPTION = +
      IF (OPTION · EQ · 1) GO TO 50
      READ(5.1) NSAMP INLAG
      READ(5,2) DELT
      DO 10 I=1:2
   10 READ(5,2) (X(J,1),J=1,NSAMP)
      wRITE(6,40) (1,X(1,1),X(1,2),1=1,NSAMP)
   40 FURMAT(2(5X,115,5X,2E2U,5))
      FORM COVARIANCES AND CORRELATIONS
      CALL COVAR (NSAMP & X & COV & MLAG)
(
      COMPUTE THE CROSS POWER SPECTRAL DENSITY
      GO TO 22
   50 READ(5,2) XEAG, DELT
       MLAG=IFIX(XLAG)
      M1=MLAG+1
      DO 21 J=1.2
      DO 21 I=1:2
   21 READ(5,2) (COV(K,1,J),K=1,M1)
   22 CONTINUE
C
      COVARIANCES ARE READ IN THE ORDER (1:1): (1:2): (2:1): (2:2)
      CALL CRSPEC (COV + MLAU + DEL I + NOAMP)
    1 FURMAT(215)
    2 FORMAT(7F10.2)
      STOP
      END
      SUBRUUTINE COVARINSAMP . X . COV . MLAG)
      DIMENSION SM(2),X(1024,2),CUV(101,2,2),0COV(101,2,2),
     1CUR(101,2,2),DCUR(101,2,2),50m(2),Xm(2)
      THE AUTU AND CROSS COVARIANCES AS WELL AS THE AUTO AND
C
      CROSS CORRELATIONS ARE COMPUTED
C
C
      COMPUTE MEAN VALUES
```

```
DO 1 J=1,2
      0.0=(L)MUZ
      DO 2 I=1.NSAMP
    2 Sum(J)=SUM(J)+X(I,J)
    1 Xm(J)=5UM(J)/N5AmP
C
      PRINT MEAN VALUES
      wRITE(6,10)
   10 FORMAT(THISSOH RESULTS OF CURRELATION COMPUTATIONS
      WRITE(6,11) (XM(J),J=1,2)
   11 FORMAT(//24H MEAN VALUE SERIES ONE = 1E20.5 /
     124H MEAN VALUE SERIES TWO = IC20.5 //)
C
      COMPUTE DEVIATIONS FROM THE MEAN
      DO 3 J=1.2
      DO 3 I=1,NSAMP
    3 X([ + ] ) X = { U e ] ) X = { U e ] ) X
C
      CUMPUTE CUVARIANCES
      M1=MLAG
      DO 4 K=1 ml
      DO 4 J=1.2
      DO 4 L=1,2
      5UM1=0.0
      MZ=NSAMP-K
      υO ⊃ I=1•m2
    5 SUM1=X(I = J) *X(I+K-1 = L) +SUM1
    4 COV(K,J,L)=SUM1/FLOAT(NSAMP)
C
       COMPUTE DIFFERENCED COVARIANCES
      DO 6 L=1.2
      D0 6 J=1.2
      DC \cup V(1, J) = -C \cup V(2, J) + 2, *C \cup V(1, J) = C \cup V(2, J, L)
      m3=m1-1
      DO 6 K=2,m3
    6 DCUV(K,J,L)=-COV(K-1,J,L)+2.*CUV(K,J,L)-CUV(K+1,J,L)
      wRITE(6,12)
   12 FORMAT(31H TABLE OF AUTO COVARIANCE (1-1)
      WRITE(6,14) (K,COV(K,1,1),K=1,4)
   14 FORMAT(4(115,5X,1F15,5,5A))
      wRITE(6.15)
   15 FORMAT(310 TABLE OF AUTO COVARIANCE (2-2)
                   (K,0COV(K,02,02),0K=1,0M1)
      wRT [E (6,14)
      wRITE(6,16)
   16 FORMAT(32H TABLE OF CROSS COVARIANCE (1-2)
      WRITE(6 = 14) (K = COV(K = 1 = 2) = K = 1 = M1)
      wKI [E(6,17)
   17 FURMAT(32H TABLE OF CRUSS COVARIANCE (2-1)
      WRITE(6,14) (K,COV(K,2,1),K=1,M1)
C
      OUTPUT DIFFERENCED COVARIANCES
```

```
WRITE (6,18)
   18 FORMAT (IH1: 46H DIFFERENCED COVARIANCES (SAME ORDER AS ABOVE)
C
      COMPUTE CORRELATIONS NORMALIZED COVARIANCES
      DOTH NORMAL AND DIFFERENCED FORMS
      DO 20 L=1+2
      DO 20 J=1.2
      COVM=SQRT(COV(1,J,J)*CUV(1,L,L))
      DCOVM=SQR1(DCGV(1,J,J)*DCOV(1,L,L))
      DO 20 K=1,M1
      COR(KaJaL)=COV(KaJaL)/COVM
   20 DCOR(K,J,L)=DCOV(K,J,L)/DCOVM
Ċ
      PRINT THE CORRELATIONS AND IDEAR DIFFERENCED FORMS
      wRITE(6,21)
   21 FORMAT(1H1,50H AUTO AND CROSS CORRELATIONS AND DIFFERENCED FORMS
     1///48H AUTO CORRETATION (WITH DIFFERENCED FORM) (1-1) //)
                   (K)COR(K)1)1)5K=19M1)
      WRIIE(6,14)
      WRITE(6,22)
   22 FURMAT(//43H AUTO CORRELATION (2-2)
      WRITE(6,14) (K,COR(K,2,2), K=1,M1)
      wRITE(6,23)
   23 FORMAT(///25H CROSS CORRELATION (1-2)
      WRITE(6,14) = (K,COR(K,1,2),K=1,0)1
      WRITE (6,24)
   24 FURMAT(///25H CRUSS CURRELATION (2-1)
      WKITE(6,14) (K,COR(K,2,1),K=1,41)
C
      THIS COMPLETES THE CORRELATION PHASE
      RETURN
      END
      JUBROUTING CROPEC (COV. MLAU, DELT. NOAMP)
C
      THE CRUSS PUNCK SPECIRAL DENSITY IS COMPUTED
      DIMENSION COV(101,2,2), COVP(101), SPECP(303), SPEC(303,2), FREW(303),
     1EV(101) , XUD(101) , SQ(303) , CUSPEC(303) , QSPEC(303) , PHASE(303) ,
     2CUHSU(303),ASPEC(303,2),DUH(ZUZ),DUP(2U2)
      DIMENSION CSPEC(303) *FREC(303)
      DAIA PI/3.14159/
      ML = MLAG
C
      FIND S WHERE S IS THE NUMBER OF TIME LAUS TO HEIGH THE TWO
C
      PROCESSES WITH MAXIMUM CURRELATION AT ZERO
      DETERMINE LAG TIME FOR SERIES ALIGNMENT
      wRITE(6,70) (COV(1,1,2,1,1,1,1,1,1)
      DO 21 K=1 MLAG
   21 DUM(K)=CUV(M1+1-K,2,1)
      DO 22 K=29m1
   22 DUMINLAG+N-1)=CUV(K+1+2)
      MM = 2 * MLAG - 1
      wRITE(6,26) \quad (I,DUM(I),I=1,MH)
                                       REPRODUCIBILITY OF THE
                                       ORIGINAL PAGE IS POOR
```

```
26 FORMAT(4(>X,115,5X,1E15,0))
      XMAX=-999.
      DO 23 K=1 MM
      DUP(K)=ABo(DUM(K))
      IF(DUP(K) GT OXMAX)
                          60 TJ 24
      GO TO 23
   24 XMAX=DUP(K)
      15=K-M1
   23 CONTINUE
      WRITE(6,25)
                   IS
   25 FURMAT(///22H ALIGNMENT LAG NUMBER
                                             1110///)
      CONDITION THE DATA FOR THE CALCULATION OF THE
C
       CRUSS SPECIRUM
      M2=M1-IAB5(I5)
Ċ
      CONDITION THE DATA FOR AUTOSPECTROM CALCULATION
      DO 20 K=192
      00 10 I=19%1
   IO COVP(I)=CUV(I,K,K)
      CALL AUSPEC (MEAUSINELTS CUVPS SPECKS FREGS 15)
C
      STURE AUTUSPECTRUM
      NF = 2 * N2 + 1
      DO 11 I=1 *NF
   11 OPEC(Isk)=OPECP(I)
   20 CONTINUE
      EV(1) = DUM(MI + IS)
      X0D(1)=0.0
      DO 40 K=2 M2
      M 44 = M1+ 15+k-1
      endeder=ad+15-K+1
      EV(K)=U。5巻(DUM(BISH)+DUM(Environ))
   40 XOD(K)=0.5*(DOM(MAN)-DOM(MANN))
      ed11c(6,70) (EV(1),000(1),1=1,02)
C
      DO THE FOURTER TRANSFORM
      CALL CROSPEC(LV=XOD+COSPEC+=SPEC+=LAU+DELT+15)
C
      COMPUTE PHASE ANGLE AND COMERTNEE FUNCTION
      RETURN CROSS SPECTROM TO UNSHIEFTED FORK
      DO 60 I=1:NF
      ARU=P1*FLOAT(1-1)*FLOAT(15)/FLOAT(NF)
      CN=CUS(ARG)
      JN=JIN(ARG)
      DUM1=COSPLC(I)*SN+QSPEC(I)*CN
      DUM2=COSPEC(I)*CN-QSPEC(I)*SN
      COSPEC(I) = DUM2
      USPEC(I)=DUM1
```

```
SQ(I) = COSPEC(I) * COSPEC(I) + QSPEC(I) * QSPEC(I)
       IF(COSPEC(I).EQ.O.O) GO TO 80
      PHASE(I)=ATAN2(-USPEC(I) *COSPEC(I))
      GO TO 81
   80 PHASE(I)=PI/2.
   81 CONTINUE
      PHASE(I)=PHASE(I)*180./PI
      CSPEC(I) = SQRT(SQ(I))
      COHod(I) = ou(I)/(opec(I + 1) * opec(I + 2))
      IF(SPEC(I)1).LE.U.U) GO TO 51
      GO TO 55
   52 CUNTINUE
      IF (SPEC(1,2), LE. U. U) GU TO 53
      GU TU 54
   51 ASPEC([,1)=-100.
      GO TO 52
   53 ASP~C(I,2)=-100.
      GO + U 60
   55 CONTINUE
      ASPEC(I \cdot I) = ALOGI \cup (SPEC(I \cdot I))
      JU 10 52
   54 CONTINUE
      ASPEC(1,2)=ALUGIU(SPEC(1,2))
   60 CUNTINUE
C
      GUNERATE THE FREQUENCY ARRAY
      コレニエ。33/(FLOA!(MLAG)*DEL!)
      JU 41 I≃1 → NF
   WRITE THE SPECTRAL LEVELS (CROSS POD) PRASE AND COHERENCY
      WRITE (6,61)
   61 FORMAT(1H1:35H RESULTS OF PURER SPECTRAL ANALYSIS
     119H AUTOSPECTRUM (1-1)
   70 FURMAT(3(3X)1F1U.4,5X,1E15.5))
      wRITE(6,70) (FREQ(I),5PLC(I,1),1=1,NF)
      WRITE (6,62)
   62 FURHAT(///19H AUTCSPECTRUM (2-2)
      wRITE(6,70) (FREQ(1),5PEC(1,2),1=1,NF)
      wRITE(6,65)
   65 FORMAT(///15H CROSS SPECTROM ///)
      wRITE(6,70) (FREQ(I),CSPEC(I),I=1,NF)
      WRITE(6,63)
   63 FURMAT(///12H PHASE ANGLE
                                 1///
      WRITE(6,70) (FREQ(I),PHASE(1),I=1,NF)
      WRITE(6,64)
   64 FORMAT(///11H COHFRENCY
                                  11/1
      *RITE(6,70) (FREQ(1),COHSQ(1),1=1,NF)
      RETURN
      END
      SUBROUTINE CRUSPEC(EV)XUD, CUSPEC, WSPEC, MLAG, DEL1, IS)
     DIMENSION EV(101),XUD(101),COOPEC(303),GOPEC(303),A(101)
      COMPUTES SMOOTHED DO- AND QUAD- SPECTRA AND SQUAREDAMPLITUDE
```

```
DATA PI/3.14159/
      ml=MLAG
      M=M1-IABS(IS)
      M2=M-1
      NF = 2*M+1
C
      COMPUTE WEIGHTS USING TUKEY WINDOW
      DO 20 J=1 M2
   20 w(J)=J.5*(1.+CO5(PI*FLUAT(J)/FLUAT(M)))
      DO 10 I=1 NF
      5UM1=0.0
      50M2=0.0
      DO 30 K=1 +M2
      ARG=PI*FLOAT(K)*FLOAT(I-1)/FLOAT(NF-1)
      SN=SIN(ARG)
      CS=COS(ARG)
      50ml=5UMl+EV(K+1)#%(K)*C5
   30 JUM2=SUM2+XOD(K+1)*W(K)*SN
      CUOPEC(1)=2.*DEL1*(EV(1)+2.*OUM1)
   10 GSPEC(I)=4.*DELT*SUM2
      RETURN
      END
      JUBRUUTINE AUSPEC (MLAG, DLL ), COV, SPEC, FREW, IS)
C
      COMPUTE AUTOSPECTRUM OF COVARIANCES
      DIMENSION COV(101) + 4(101) + 5PEC(303) + FREU(303)
      DATA PI/3.14159/
\mathsf{C}
      THE TUKEY WINDOW IS USED FOR DATA SMOOTHING
      COMPUT WEIGHTS
      M1=HLAG
      M=M1-IABS(IS)
      142=14-1
      NF = 2 \times M + 1
      Mel=I Oi UG
   10 "(I)=0.5*(1.+CO5(PI*FLOA!(I)/FLOA!(M)))
C
      CALCULATE A SMOOTHED AUTOSPECTRAL ESTIMATE
      MM = M + 1
      00 20 I=1•NF
      JUM=0.∪
      DO 21 K=1:MM
      ARG=PI*FLOAT(K)*FLOAT(I-1)/FLOAT(NF-1)
      VAR=COV(K+1)*W(K)*COS(ARG)
   21 SUM=SUM+VAR
   20 SPEC(1)=2.*DELT*(COV(1)+2.*SUM)
      COMPUTE BANDWIDTH AND DEGREES OF FREEDOM
C
      RETURN
      END
```